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A STUDY OF THE EFFECTS  
OF VARYING RATES OF LOADING  
ON THE CONSOLIDATION OF SOIL

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ROBERT K. WHITE

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A STUDY OF THE EFFECTS OF VARYING RATES OF LOADING ON  
THE CONSOLIDATION OF SOIL

by

Robert K. White

A Thesis Submitted to the Faculty  
of the Department of Civil Engineering  
in Partial Fulfillment of the  
Requirements for the Degree of  
MASTER OF CIVIL ENGINEERING

Approved:

---

Adviser

Rensselaer Polytechnic Institute

Troy, New York

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TABLE OF CONTENTS

|  | Page |
|--|------|
| LIST OF TABLES                           | v    |
| LIST OF FIGURES                          | vi   |
| FOREWORD                                 | vii  |
| ABSTRACT                                 | viii |
| I. INTRODUCTION.....                     | 1    |
| A. Objective.....                        | 1    |
| B. Historical Revue.....                 | 2    |
| II. THEORY.....                          | 4    |
| A. General.....                          | 4    |
| B. Theory of Terzaghi.....               | 5    |
| C. Research by Taylor.....               | 12   |
| D. Extension to Theory by Schiffman..... | 13   |
| III. MATERIALS AND APPARATUS.....        | 15   |
| IV. METHOD OF PROCEDURE.....             | 21   |
| A. Preparation of Sample.....            | 21   |
| B. Static Loading Test.....              | 24   |
| C. Time-Dependent Loading Test.....      | 25   |
| D. Permeability Measurements.....        | 29   |
| V. RESULTS.....                          | 30   |
| VI. DISCUSSION.....                      | 43   |
| A. Static Tests.....                     | 43   |
| B. Time-Dependent Loading Tests.....     | 45   |
| C. General.....                          | 47   |
| VII. CONCLUSIONS.....                    | 49   |
| VIII. LITERATURE CITED.....              | 50   |



|   | Page |
|---|------|
| IX. APPENDICES.....                                     | 51   |
| A. Sample Raw Data, Static Test.....                    | 51   |
| B. Sample Raw Data, Time-Dependent<br>Loading Test..... | 58   |



## LIST OF TABLES

|         |                                   |            |
|---------|-----------------------------------|------------|
| Table 1 | Continuous Loading Test Data..... | Page<br>23 |
|---------|-----------------------------------|------------|



## LIST OF FIGURES

|  | Page |
|--|------|
| Figure 1      The Consolidation Process.....   | 7    |
| Figure 2      Consolidation as a Function of Depth and<br>Time Factor.....                         | 9    |
| Figure 3      Degree of Consolidation Versus Time Factor   | 9    |
| Figure 4      Graphical Method of Determining Time Fac-<br>tor for Non-Instantaneous Loadings..... | 11   |
| Figure 5      Standard Fixed Ring Consolidometer.....  | 16   |
| Figure 6      Continuous Loading Device.....   | 17   |
| Figure 7      Time-Dependent Loading Mechanism.....  | 19   |
| Figure 8      Constant Head Permeameter.....   | 20   |
| Figure 9      Atterberg Flow Curve.....  | 22   |
| Figure 10     Humidifier.....  | 23   |
| Figure 11     Bellows Calibration Curve.....   | 26   |
| Figure 12     Bellows Spring Constant.....   | 27   |
| Figure 13     Void Ratio Vs. Logarithm of Pressure.....  | 31   |
| Figure 14     Void Ratio Vs. Time for Time-Dependent<br>Loading.....                               | 32   |
| Figure 15     Void Ratio Vs. Time for Static Loading....   | 33   |
| Figure 16     Total Strain Vs. Time for Time-Dependent<br>Loading.....                             | 35   |
| Figure 17     Total Strain Vs. Loading Rate for Time-<br>Dependent Loading.....                    | 36   |
| Figure 18     Total Strain Vs. Time for Static Loading..   | 37   |
| Figure 19     Permeability Vs. Porosity for Static<br>Loading.....                                 | 39   |
| Figure 20     Permeability Vs. Porosity for Time-Depen-<br>dent Loading.....                       | 40   |
| Figure 21     Permeability Vs. Logarithm of Time for<br>Static Loading.....                        | 41   |





## FOREWORD

From his first introduction to the subject of soil mechanics, one is impressed most, perhaps, by the profusion of unknown or questionable factors involved in accurately predicting soil behavior. For this reason, attempts at formulization of these unknowns are of primary interest. This impression, more than any other factor, served as a stimulus for undertaking the investigation reported in this thesis.

The author would like to express his appreciation to Assistant Professor Robert L. Schiffman who, as adviser, aided greatly in the setting up and conduct of the experimental program.

In addition, the author is indebted to the Division of Soil Mechanics, headed by Professor E. J. Kilcawley, for their very able and courteous assistance both by providing hints and suggestions and also by making available the facilities of the entire section. This assistance was invaluable.



## ABSTRACT

In order to predict more accurately the settlement of structures, many approaches to the theory of consolidation have been made. The most famous of these is the Terzaghi theory. The limitations of this theory as associated with construction loading have been recognized by Schiffman in his approach to a mathematical solution. Marron initiated investigations into the validity of Schiffman's work, and it is the purpose of this investigation to further these studies.

Testing was carried out on two types of apparatus. The first one, a standard, two-position static loading device, was utilized during three series of tests including a usual incremental test, a large incremental test, and a small incremental test.

The second apparatus consisted of a Conbel loading device which was operated by air pressure regulated through a valve which in turn was connected to an opening mechanism. This opening mechanism consisted of a geared-down electric motor whose output rate could be varied by a belt-and-pulley arrangement to the valve stem. Thirteen test runs at varying rates were conducted with this device.

Permeability readings were conducted throughout testing by use of a constant head permeameter developed by Marron.



The material used throughout testing was a pure kaolinite clay, the inclusion of which it was hoped would eliminate many of the inconsistencies encountered in a natural soil. Thus, results would be that much more easily interpreted.

The results of this experimentation show that there is a definite effect upon total strain and void ratio change by imposition of different loading conditions. It can definitely be seen that large increments and more rapid loading rates cause larger deformation.

For the static tests it was seen that larger permeabilities were experienced at the same porosity when large increments were applied than when small increments were applied.

During the time dependent loading tests, the results failed to show any definite relationship between permeability and porosity, though the fact that there was a spread of values leads to speculation that further, more intensive study along this line would be warranted.

It is concluded that as far as the scope of this study has investigated, Schiffman's approach to the consolidation of soil under conditions of time-dependent loading and varying permeability is valid.



PART I.  
INTRODUCTION

A. Objective

The purpose of a study of soil mechanics is to be better able to predict the behavior of soil under varying conditions encountered in the field. One aspect of soil behavior quite important in all construction is the process of consolidation and just how much settlement can be expected after the construction takes place and a load is applied.

The studies by Dr. Karl Terzaghi in this field are almost universally followed. However, many investigators have recognized certain shortcomings therein and have attempted to extend Terzaghi's theory with modifications to take care of these shortcomings.

Very recent work by Assistant Professor Robert L. Schiffman of Rensselaer Polytechnic Institute has presented a mathematical solution to consolidation under conditions of time-dependent loading and varying permeability. It is considered that such conditions more accurately approximate actual field situations.

It is the avowed purpose of this study to conduct a series of consolidation tests under various rates of loading. Perhaps, not as a direct result of these tests alone but after a period of extended study, Schiffman's and/or similar approaches can be completely validated. Thus, the practice of soil mechanics will become more nearly a science.





## B. Historical Review

Dr. Karl Terzaghi, in one of his works (9) states that in 1856 Tyndall discussed "partially consolidated mud" in his "Fragments of Science". For the next few decades work done in the direction of consolidation was mostly as connected with agriculture. However, to illustrate that the problems of consolidation were still being studied by the pioneers in the field, Collingwood (1) in 1891, at a lecture presented at Rensselaer Polytechnic Institute, stated that subsurface exploration should be carried out to such a depth as to preclude the possibility of the presence of a compressible layer.

However, all of these statements and all the empirical formulae previously developed were shoved into obscurity when in 1925 Dr. Terzaghi (8) published his "Theory of Consolidation". For the first time engineers had at their disposal a quantitative method of predicting consolidation under loading. Since 1925 there have been innumerable treatises either extending, criticising, or upholding Dr. Terzaghi's work (2, 3, 5, 6, 10), but to this day his theory is still the basis of all work in the field.

The most questionable of Dr. Terzaghi's original assumptions, however, is that of instantaneously applied loading, and although graphical approximations to time rates of loading and total settlement have been developed, there has been no rigorous mathematical solution to the problem.



Schiffman (5) has attempted this mathematical approach recently, and Marron (4) initiated laboratory work in an attempt to justify Schiffman's approach. In this work, the author intends to further these studies of Marron.



## PART II.

## THEORY

A. General

It is generally acknowledged that the most valid theory of consolidation of soils is that proposed by Dr. Karl Terzaghi (8) in 1925. There is actually little point in bringing forth any theory introduced prior to this time. Since this important contribution of Dr. Terzaghi, however, there have been certain modifications and extensions proposed (5, 7) and it might be well to mention them.

Further, although it is understood that many volumes of theory could be included as being pertinent, the author has no intention of restating much of the fundamental work which is readily available in almost any standard textbook on soil mechanics.



### B. Theory of Terzaghi

The assumptions stated by Dr. Terzaghi in the presentation of his theory are as follows:

1. Homogeneous soil
2. Voids of the soil are completely filled with water
3. Water and solid constituents of soil are completely incompressible
4. Darcy's law is strictly valid
5. The coefficient of permeability  $K$  is a constant
6. The time lag of consolidation is due entirely to the low soil permeability
7. The clay is laterally confined
8. Both the total and effective normal stresses are the same for every stage of the process of consolidation
9. An increase in the effective pressure from an initial value  $\bar{p}_0$  to a final value  $\bar{p}$  reduces the void ratio of the clay from an initial value  $e_0$  to a final value  $e$ . The ratio

$$a_{vc} = \frac{e_0 - e}{\bar{p} - \bar{p}_0}$$

is assumed a constant for the range of pressure  $\bar{p}_0$  to  $\bar{p}$ .  $a_{vc}$  is called the coefficient of compressibility.

Using these assumptions and considering a layer

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of clay buried beneath a bed of highly permeable sand with a uniformly distributed surcharge instantly applied to the surface of the sand (Figure 1), Dr. Terzaghi developed the following differential equation:

$$\frac{\partial u}{\partial t} = \frac{K}{\gamma_w m_{vc}} \frac{\partial^2 u}{\partial z^2}$$

in which,

$u$  = excess pore pressure

$t$  = time

$K$  = the coefficient of permeability

$\gamma_w$  = the unit weight of the water

$m_{vc} = \frac{a_{vc}}{1+e_0}$  = the coefficient of volume decrease

$z$  = vertical distance

For simplification, the relation

$$\frac{K}{\gamma_w m_{vc}} = C_{vc}$$

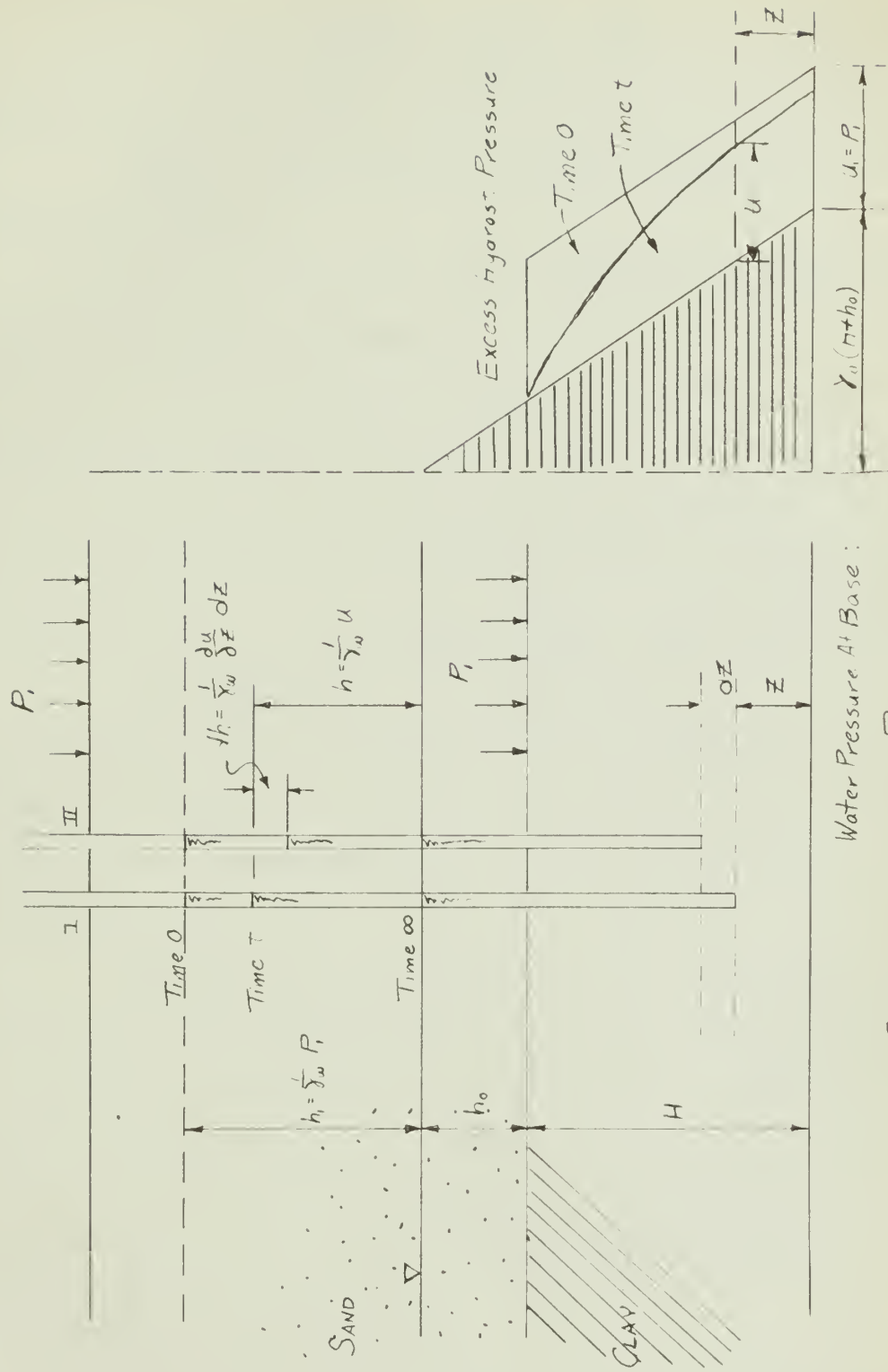
where  $C_{vc}$  becomes the coefficient of consolidation.

It is interesting to note that the process of consolidation as brought forth by Dr. Terzaghi has been shown to have mathematical analogues with the following physical processes: heat transfer, diffusion of substances dissolved in liquids, diffusion of gases, propagation of electric currents in cables, and movement of solid bodies through a stationary viscous liquid. (9)

For the boundary conditions stated and by use of Fourier's series, Dr. Terzaghi's differential equation leads to the following equation:

$$u = \frac{4}{\pi} p_0 \sum_{N=0}^{\infty} \frac{1}{2N+1} \sin \left[ \frac{2(N+1)\pi z}{H} \right] e^{-\frac{(2N+1)^2 \pi^2 C_{vc} T}{4H^2}} \quad (1)$$





Water Pressure At Base:

CONSOLIDATION PROCESS

Figure 1



The relationship

$$T_v = \frac{C_v}{H^2} t = \frac{K}{\gamma_w m_v} \times \frac{t}{H^2}$$

represents an independent variable called the "time factor".

However, the ultimate purpose of the theory is to predict settlement.

The decrease  $dp$  of the thickness of a horizontal layer of original thickness  $dz$  is:

$$dp = \Delta n dz = m_v (p_i - u) dz$$

Therefore settlement  $P$  at time  $t$  is:

$$P = \int_0^H \Delta n dz = m_v (p_i H - \int_0^H u dz) \quad (2)$$

Substituting this value in equation (1) and integrating results in:

$$P = m_v p_i H \left[ 1 - \frac{8}{\pi^2} \sum_{N=1}^{\infty} \frac{1}{(2N+1)^2} e^{(-2N+1)^2 \pi^2 \frac{T_v}{4}} \right] \quad (3)$$

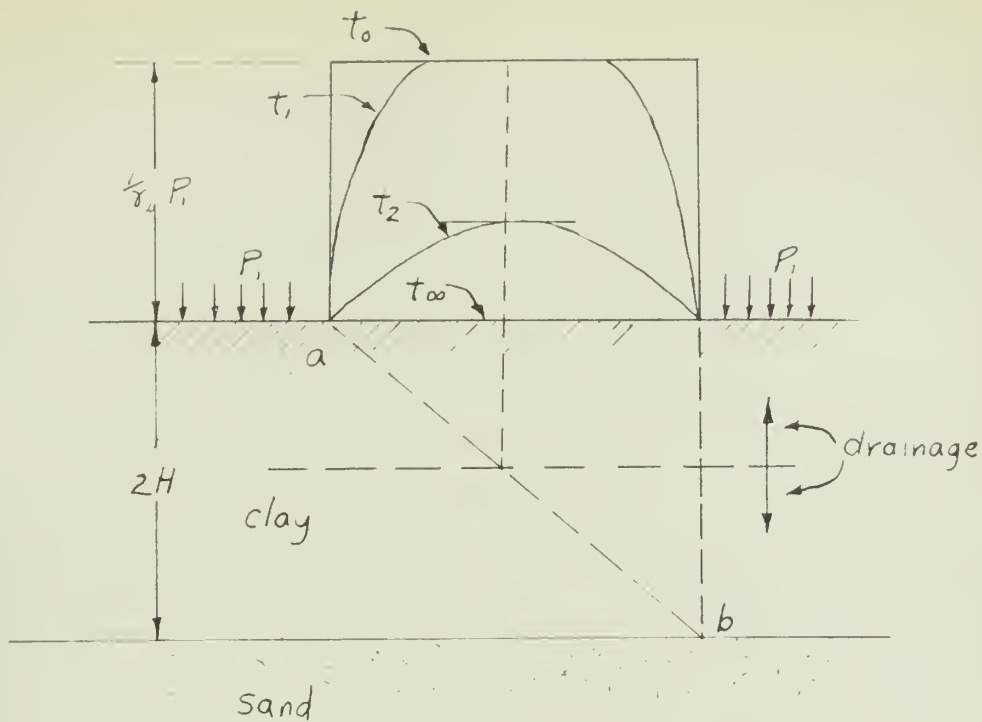
it can be seen that the factor outside the brackets represents the ultimate settlement, for as time  $t$  approaches infinity, the right-hand side of the relationship in brackets approaches zero.

However, it is not necessary in most cases to go through all these computations, since Terzaghi and Frohlich (9) plotted a family of curves (Figure 2) to approximate various loading conditions. Thus the process of predicting a reasonable value of settlement at a particular time is greatly simplified. First, the ultimate settlement is computed using the relationship:

$$P_i = H m_v p_{avg}$$

Next, the time factor  $T_v$  is calculated, and using this in





Consolidation of clay layer after sudden application of uniformly distributed surcharge. Curves show locus of water level in vertical piezometric tubes whose lower ends are located on  $\overline{ab}$ .

Figure 2

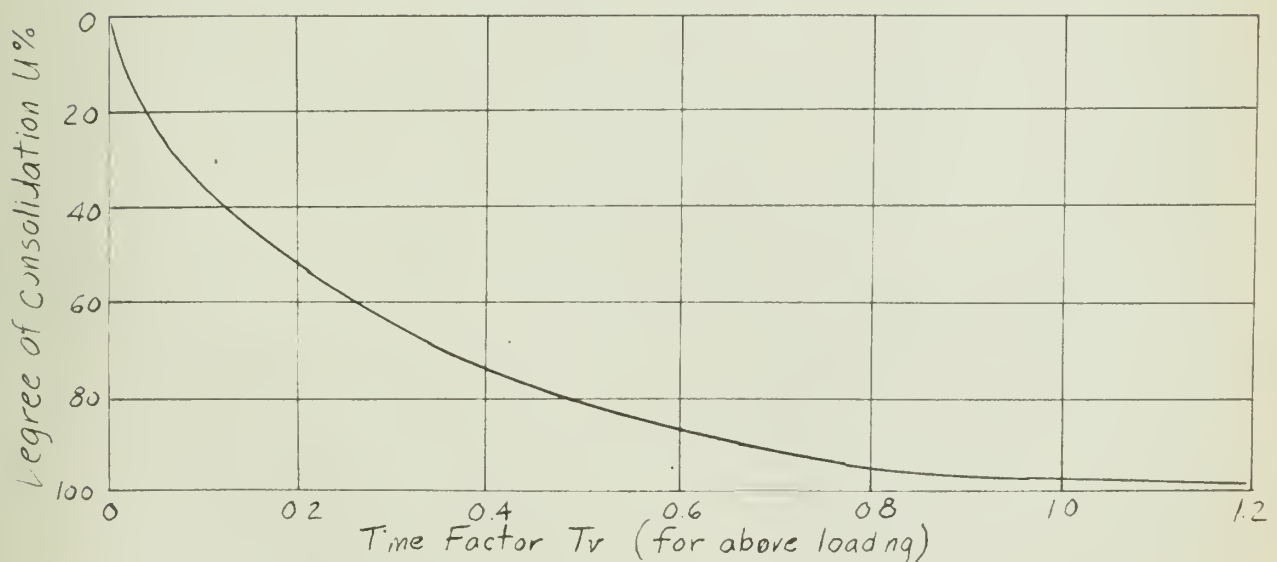


Figure 3





the chart of time factor versus degree of consolidation (Figure 3) a value of  $U\%$  is arrived at.

Therefore, the settlement at the particular time  $t$  is merely

$$P = P_1 \left( \frac{U\%}{100} \right)$$

However, one important fact has been overlooked thus far. Very seldom in the field is a load instantaneously applied and not subsequently increased. Recognizing this fact, Terzaghi and Frohlich (9) developed a graphical method. This is pictured in Figure 4. The phenomenon of linear load increase is exemplified, but other conditions of gradual load application are set forth in Terzaghi and Frohlich (9).



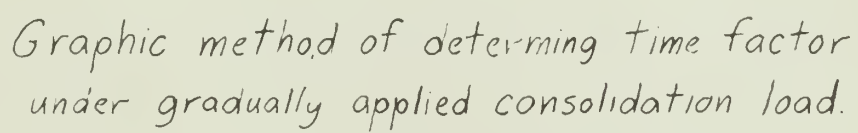


Figure 4



### C. Research by Taylor

D. W. Taylor published in 1942 (7) the results of several years' study of the consolidation of clays. The outcome of the studies was an indication that settlement predictions based upon the data of conventional consolidation tests are likely to be seriously in error unless the increments of load for the test and the actual structure are essentially alike. In other words, the research indicated that the consolidation relationship is not independent of the loading increment as Dr. Terzaghi's theory indicates. In conclusion, Taylor (7) stated that his results were conclusive enough to show that a need existed for more study into the factors which vary during consolidation.



#### D. Extension to Theory by Schiffman

Schiffman presents in (5) a mathematical approach to the condition of time-dependent loading and varying permeability of soil. His basic assumptions are:

1. Soil mass is completely saturated, the fluid incompressible, and the soil is of incompressible particles of small size
2. Darcy's law is instantaneously valid
3. The change in volume is small as compared to the original volume and is linear

Next he develops a differential equation of the general theory of consolidation with varying permeability and time-dependent loading and presents it in three forms as follows:

$$(1) \quad a \nabla u^2 + \nabla u \cdot \nabla K_f + a u \nabla^2 u + K_f \nabla^2 u + \phi \gamma_w = m \gamma_w \frac{\partial u}{\partial t}$$

$$(2) \quad \frac{1}{2} (\nabla K)^2 - \frac{1}{2} (\nabla K \nabla K_f) + \frac{1}{2} K \nabla^2 K - \frac{1}{2} K \nabla K_f + \phi \gamma_w = \frac{m \gamma_w}{a} \frac{\partial K}{\partial t}$$

$$(3) \quad \nabla K_0 \nabla u - a (\nabla u_0 - \nabla u) + a (\nabla u)^2 + a u \nabla^2 u + (K_0 + a u_0) \nabla^2 u + \phi \gamma_w = m \gamma_w \frac{\partial u}{\partial t}$$

However, the condition most closely approximated by the standard consolidation test is so-called one-dimensional consolidation. Under one-dimensional consolidation the following working conditions are evident:

- (1) doubly drained clay layer
- (2) clay layer of finite thickness





- (3) clay layer infinite in width and breadth
- (4) loading on the surface is infinite in extent
- (5) the initial coefficient of permeability is uniform throughout clay layer
- (6) initially imposed excess pore pressure is uniform throughout clay layer

Using these limiting conditions, the differential equation becomes:

$$\left[ C_0 + \frac{a u_0}{m \gamma_w} \right] \frac{\partial^2 u}{\partial z^2} - \frac{a}{m \gamma_w} u \frac{\partial^2 u}{\partial z^2} - \frac{a}{m \gamma_w} \left( \frac{\partial u}{\partial z} \right)^2 + R = \frac{\partial u}{\partial t}$$

in which

- $R =$  rate of change of imposed excess pore pressure
- $C_0 =$  coefficient of consolidation at beginning of consolidation



## PART III.

## MATERIALS AND APPARATUS

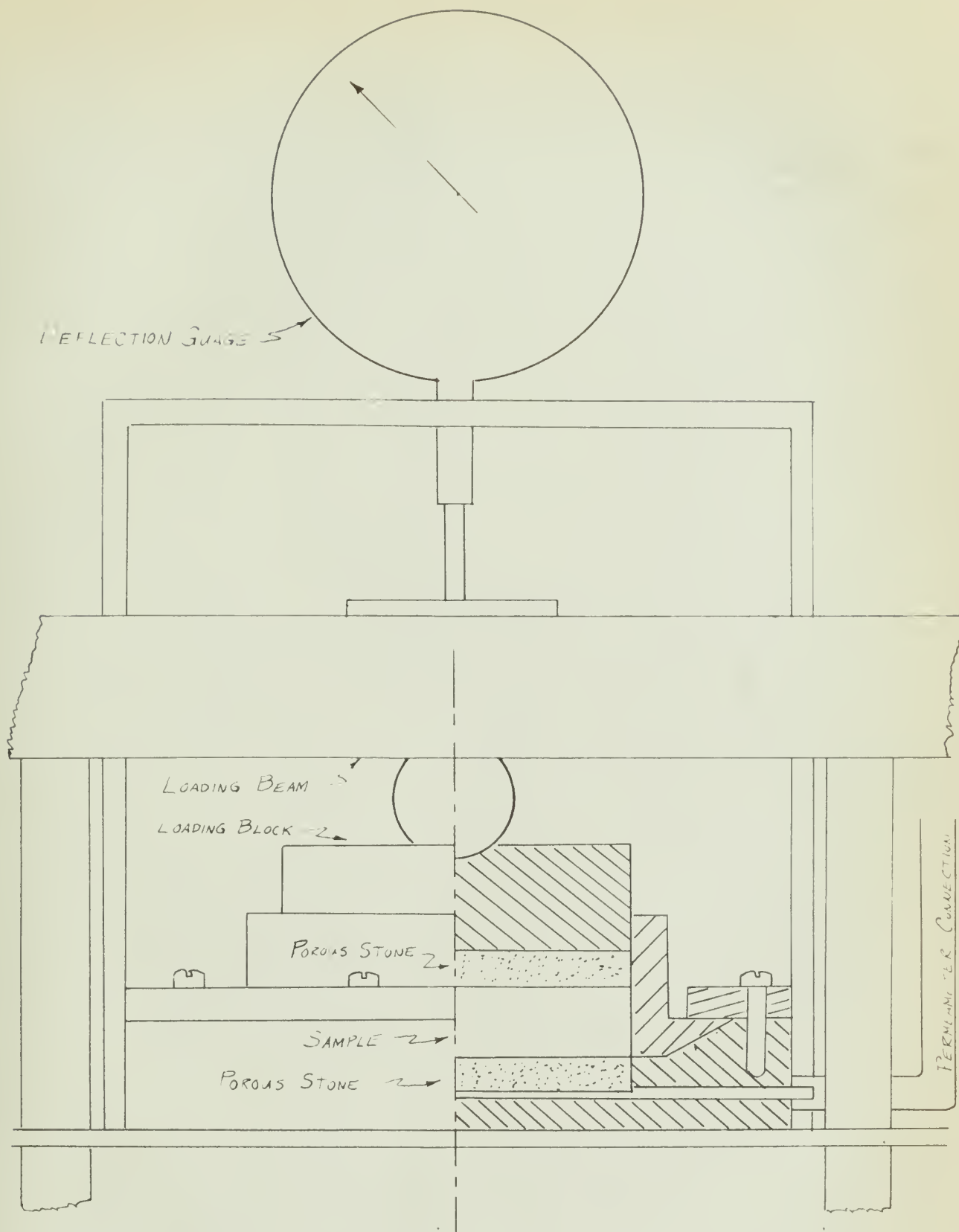
The soil samples used during this investigation were prepared from pure kaolin clay received from Ward's Natural Science Corporation, Rochester, New York. The sample designation was "Kaolinite--Dry Branch Ga. Dana #492". An attempt to magnify the permeability readings by using samples composed of 50% kaolin and 50% of a sifted silt was abandoned when it was discovered that the readings were virtually unchanged.

Throughout the testing program a standard  $2\frac{1}{2}$ " fixed ring consolidometer as shown in Figure 5 was used. The sample was separated from the porous stones by filter paper sheets which tended to prevent clogging the pores of the stones.

Loading during the static tests was applied by use of a Soil-Test Model C-280 beam loading device which afforded two positions for running duplicate tests.

Loading during the continuous loading test was applied by use of a Conbel Model 350 as shown in Figure 6. This apparatus was adapted to continuous loading by placing a Conoflow regulator valve in the line supplying air pressure to the pressure accumulator of the Conbel equipment. This valve was gradually opened by means of a belt and pulley arrangement connected to a gear train and driven by a



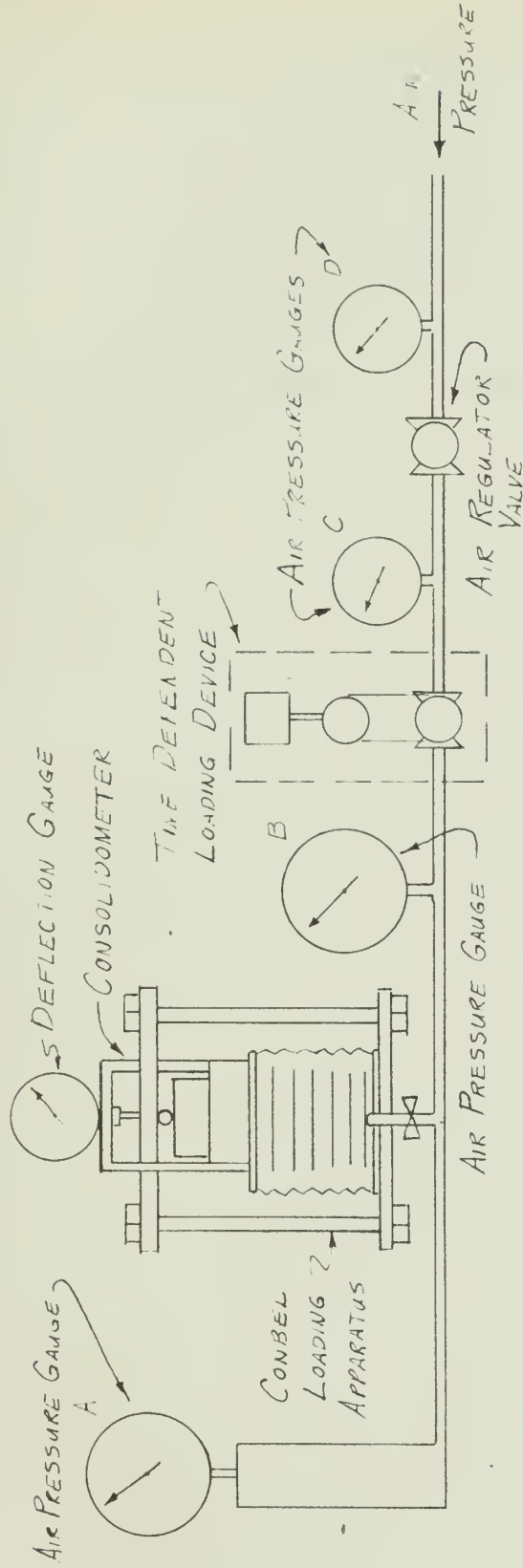


STANDARD FIXED RING CONSOLIDOMETER (FULL SCALE)

Figure 5



# CONTINUOUS LOADING DEVICE



## OPERATING PROCEDURE

1. Close Air Regulator Valves
2. Turn On Air Pressure.
3. Open Air Regulator Valve To Set Maximum Air Pressure Desired on Gauge C.
4. Set Time-Dependent Loading Device So That Gauge B Reads Zero.
5. Insert Consolidometer in Concel Apparatus, Take Up Lost Motion Between Loading Head And Consolidometer, Set Deflection Gauge To Zero.
6. Start Time-Dependent Loading Device, At Times t Read Air Pressure on Gauge A While Checking Against Gauge B, And Read Deflection Gauge.

Figure 6

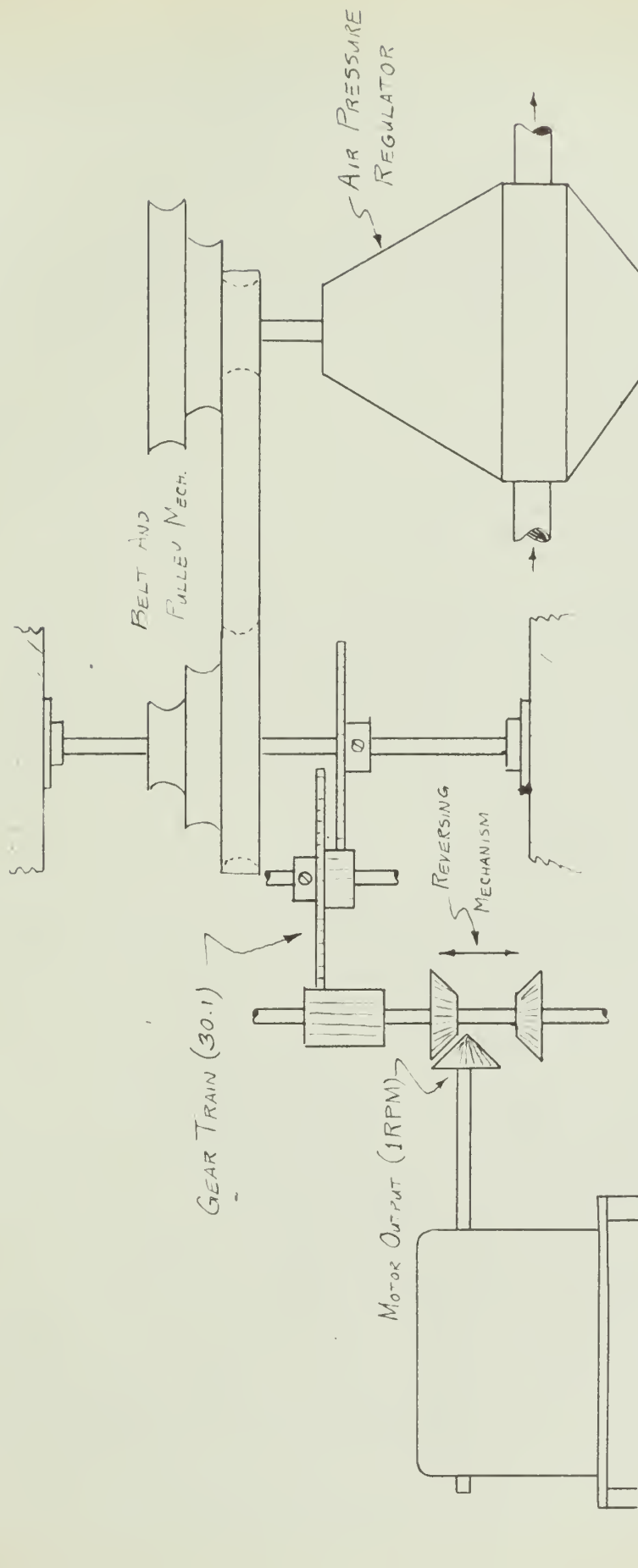




Holtzer-Cabot electric motor (9 watt--75 oz.-in. torque) as shown in Figure 7, which in turn was geared down to one revolution-per-minute. Various rates-of-opening the valve were obtained by varying the pulley ratios.

Permeability readings throughout all tests utilized a constant head permeameter as shown in Figure 8.



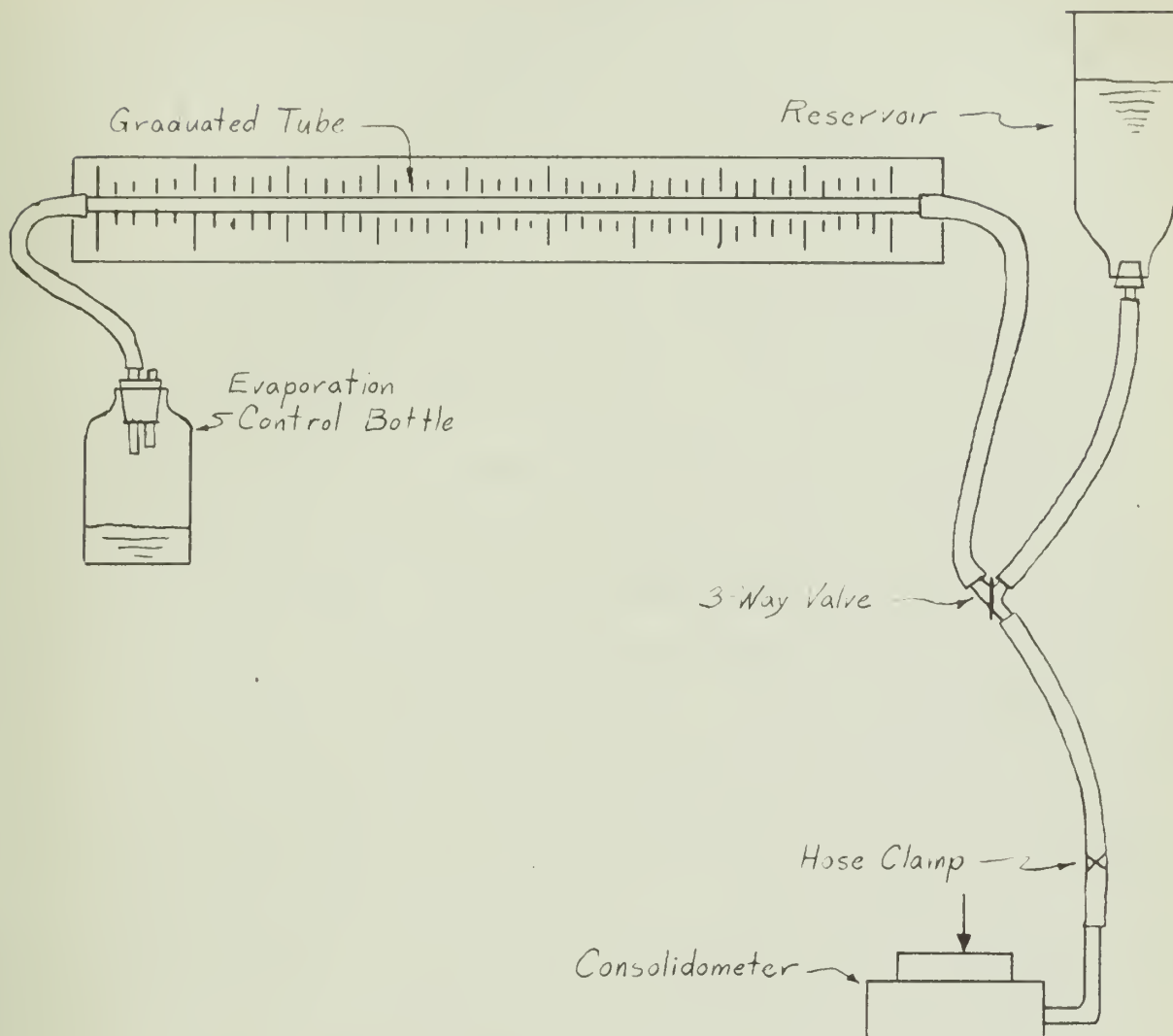


TIME-DEPENDENT LOADING DEVICE (Schematic)

Figure 7



## CONSTANT HEAD PERMEAMETER



### OPERATING PROCEDURE

1. Attach Hose To Consolidometer With Hose Clamp Attached And With 3-Way Valve Closed To Graduated Tube, Making Sure That No Air Bubbles Are Trapped In Consolidometer.
2. Open 3-Way Valve To Graduated Tube And Allow Water To Flow Into Evaporation Control Bottle Until All Air Bubbles Are Purged From System.
3. Close Three Way Valve To Reservoir, Open Hose Clamp, And Set Zero Reading On Graduated Tube.

Figure 8



## PART IV.

## METHOD OF PROCEDURE

A. Preparation of Sample

Preparation of samples was at the liquid limit which was computed according to ASTM Standards. The flow curve from this determination is shown in Figure 9. This agreed favorably with the value determined by Marron (4), so only one value was computed. Mixing was accomplished by adding distilled water to 150 grams of dry kaolin and blending with a standard spatula. Enough water was added to bring the moisture content to approximately 3% above the liquid limit (44%). After blending was complete, the sample, in a porcelain evaporating dish, was placed in dessicator which had been converted to a humidifier by removing the dessicant and placing water in the bottom. This aging period lasted twelve hours and was meant to permit a more thorough saturation of the sample, thus more closely approximating a homogeneous material. The humidifier is shown in Figure 10.

The sample was placed in the consolidometer as set forth by Marron (4), but it was especially attempted to equalize for each sample preparation the periods utilized in removing entrapped air. Again, it was thought that a closer approach to homogeneity of all samples throughout the testing would be gained by standardization of the preparation procedure.





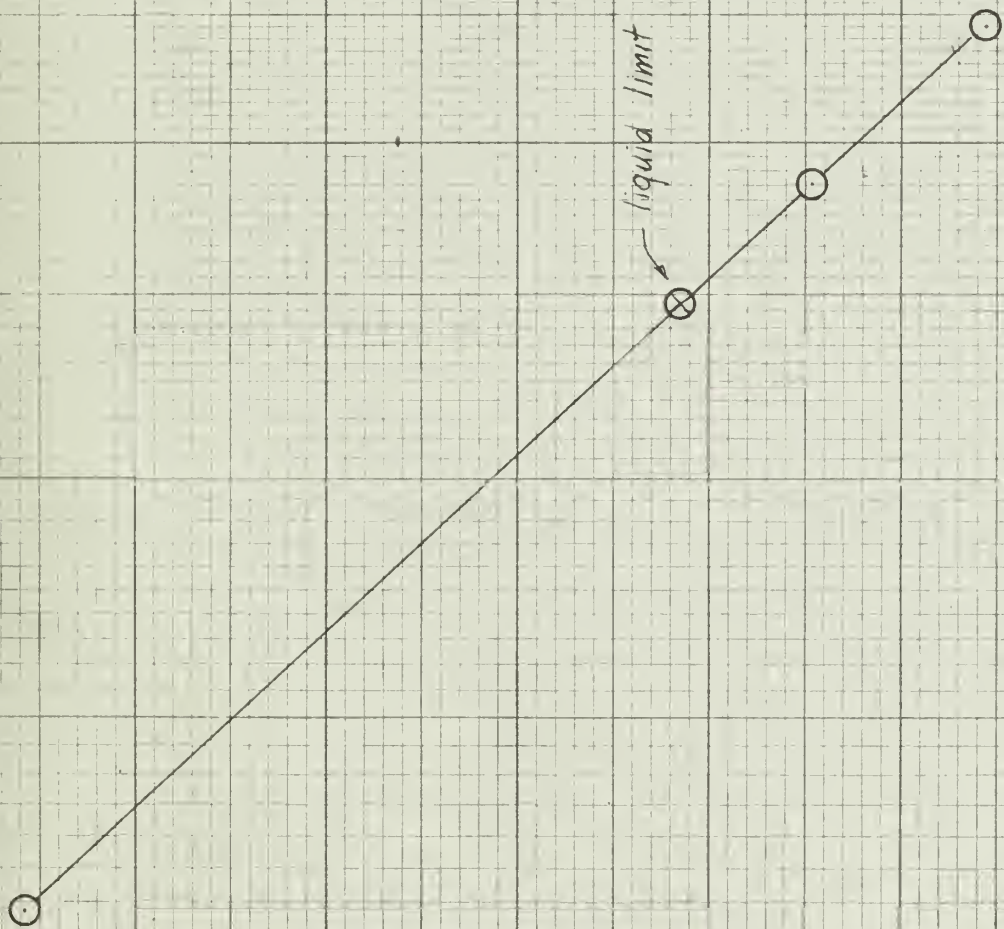
Atterberg Flow Curve  
for  
Pure Kaolin Clay

Figure 9

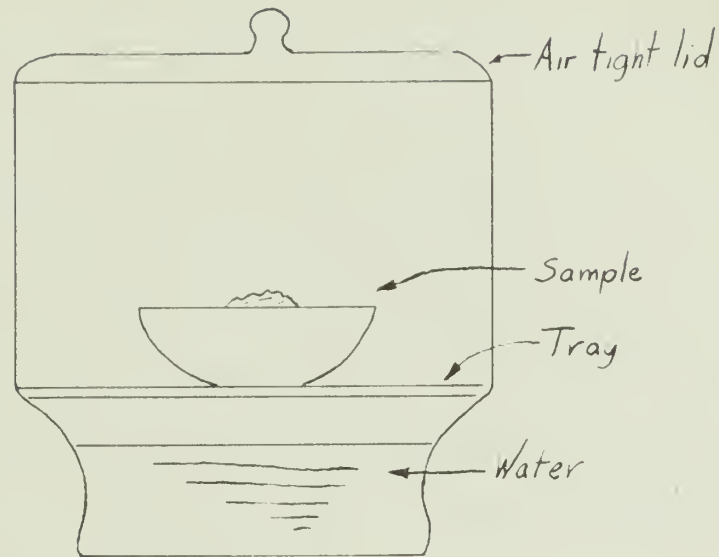
% Moisture

liquid limit

No. of Blows







### Humidifier

Figure 10

| Test # | Loading Rate $\frac{TSF}{HR}$ | Final Load (TSF) |
|--------|-------------------------------|------------------|
| 1      | 2.15                          | 15.45            |
| 2      | 2.07                          | 9.50             |
| 3      | 1.89                          | 13.20            |
| 4      | 2.00                          | 13.27            |
| 5      | 1.78                          | 15.50            |
| 6      | 1.78                          | 13.28            |
| 7      | 2.15                          | 15.80            |
| 8      | 1.20                          | 14.80            |
| 9      | 1.32                          | 13.25            |
| 10     | 1.10                          | 15.48            |
| 11     | 2.50                          | 12.81            |
| 12     | 2.75                          | 13.80            |
| 13     | 2.21                          | 11.60            |

### Continuous Loading Data

Table I



### B. Static Loading Test

Three series of static loading tests were run. The first, the so-called "usual test", was run as a pilot study to establish procedures and to become acquainted with the equipment. Increments of loading were as follows (Tons per Square Foot): 0-1/4, 1/4-1/2, 1/2-1, 1-2, 2-4, 4-8.

The second test was labeled the small increment test and consisted of loadings as follows: 0-1/4, 1/4-1/2, 1/2-1, 1-1 1/2, 1 1/2-2, 2-2 1/2, 2 1/2-3, 3-3 1/2, 3 1/2-4, 4-4 1/2, 4 1/2-5, 5-6, 6-7, 7-8.

The third test was labeled the large increment test and consisted of loadings as follows: 0-1/2, 1/2-1, 1-2, 2-4, 4-8.

A sample data sheet is contained in Appendix I.

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1900

### C. Time-Dependent Loading Test

A total of thirteen continuous loading tests were run. However, at the beginning of testing it was noted that the bellows had a slight permanent tilt to it. Upon application of load it became more canted until it no longer imposed an axial load upon the specimen. Therefore, a new bellows was procured. As a result, calibration became necessary. Calibration was simplified considerably from that mentioned by Marron (4) by use of a standard materials testing machine. Procedure was as follows: The bellows was placed in the machine so to prevent vertical expansion upon applying air pressure to the bellows. Air pressure was then gradually increased up to the maximum available in the local air system, and a plot was made of this air pressure versus the pressure exerted by the testing machine, read directly off the machine dial in pounds. This calibration agreed precisely with that of the former bellows. The calibration curve is shown in Figure 11. The spring constant was determined by attaching a spring scale to the bellows, exerting a vertical load while plotting the vertical expansion of the bellows versus the load in pounds read from the spring scale. This curve is shown in Figure 12.

The procedure for operating this equipment is set forth in Figure 6, and is supplemented by information in the Materials and Apparatus section of this paper.



THE HISTORY OF THE

REIGN OF KING CHARLES THE FIRST

IN THE YEAR OF HIS REIGN 1625

BY JOHN BURNET

IN TWO VOLUMES

LONDON

Printed by J. Streater, at the Sign of the Gun, in St. Dunstons Church-yard

1725

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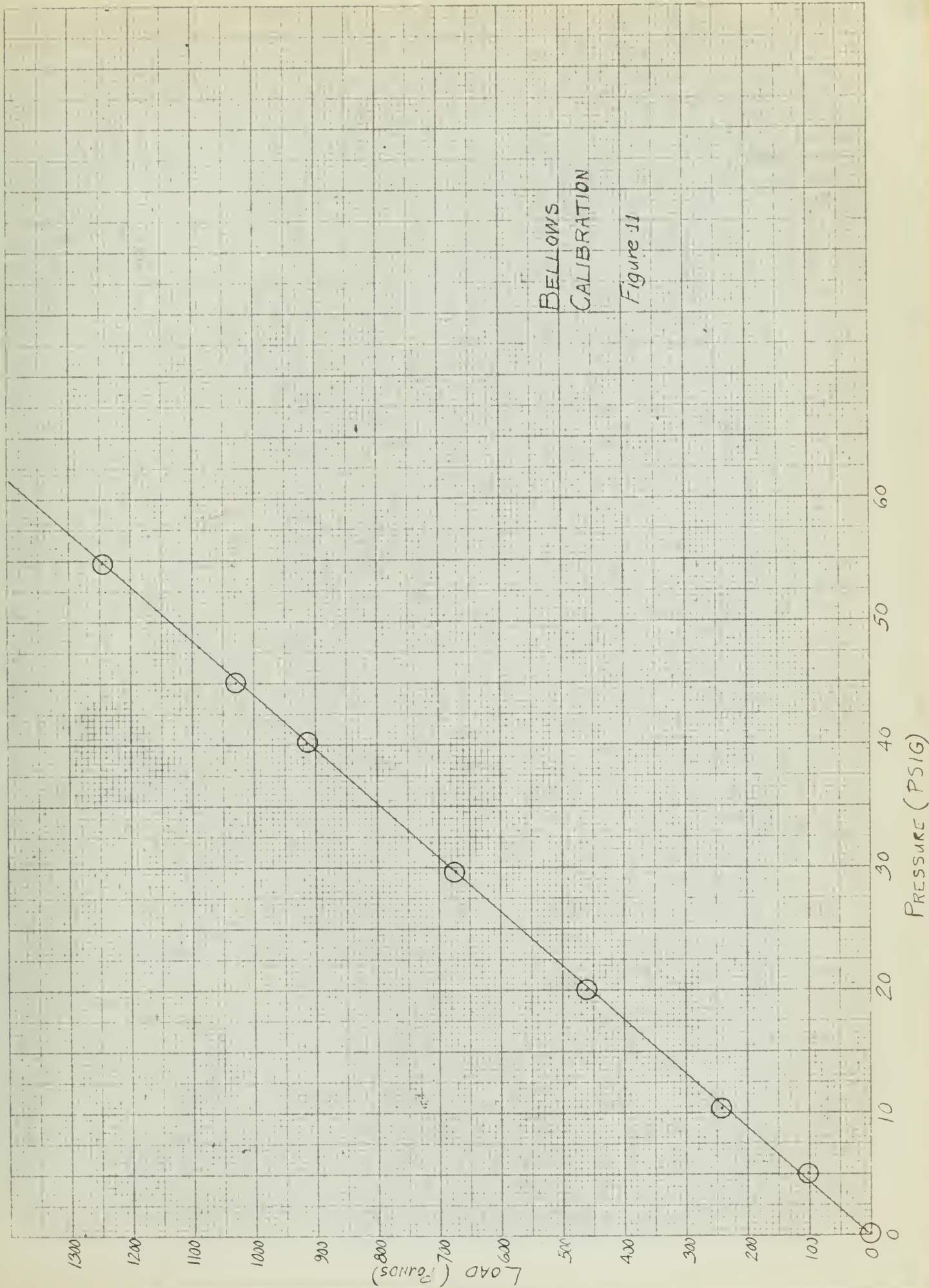
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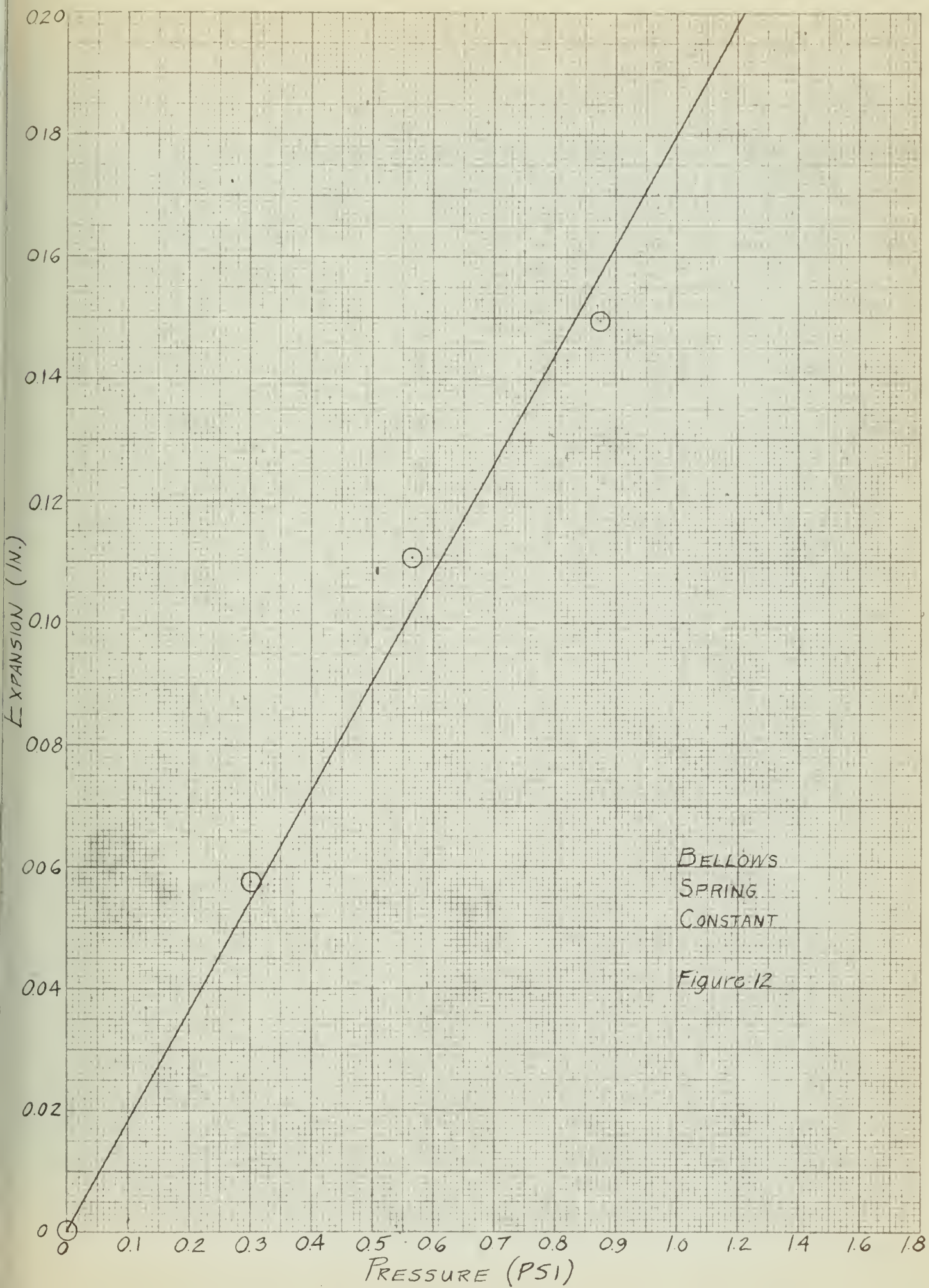




BELLOWS  
CALIBRATION

Figure 11









The rates of loading, and final loads imposed are set forth in Table 1. Sample data sheets are included in Appendix II.



#### D. Permeability Measurements

Permeability readings were taken throughout the testing runs as far as practicable. A constant head permeameter as depicted in Figure 8 was used. The procedure for utilizing this permeameter is also included on Figure 8.

Since considerable head was utilized in this permeameter there was necessarily a delay before permeability readings could be taken. As set forth in Marron (4) sample uplift occurs. It will also be noted that readings were taken during the process of consolidation even though it was realized that values of  $K$  (coefficient of permeability) computed from these readings would be false. It was thought, however, that some relationship between the rate of loading and the variations of these computed values might become evident.





## PART V.

## RESULTS

Data from the three series of static tests and the twelve runs are presented graphically in Figures 13 through 20.

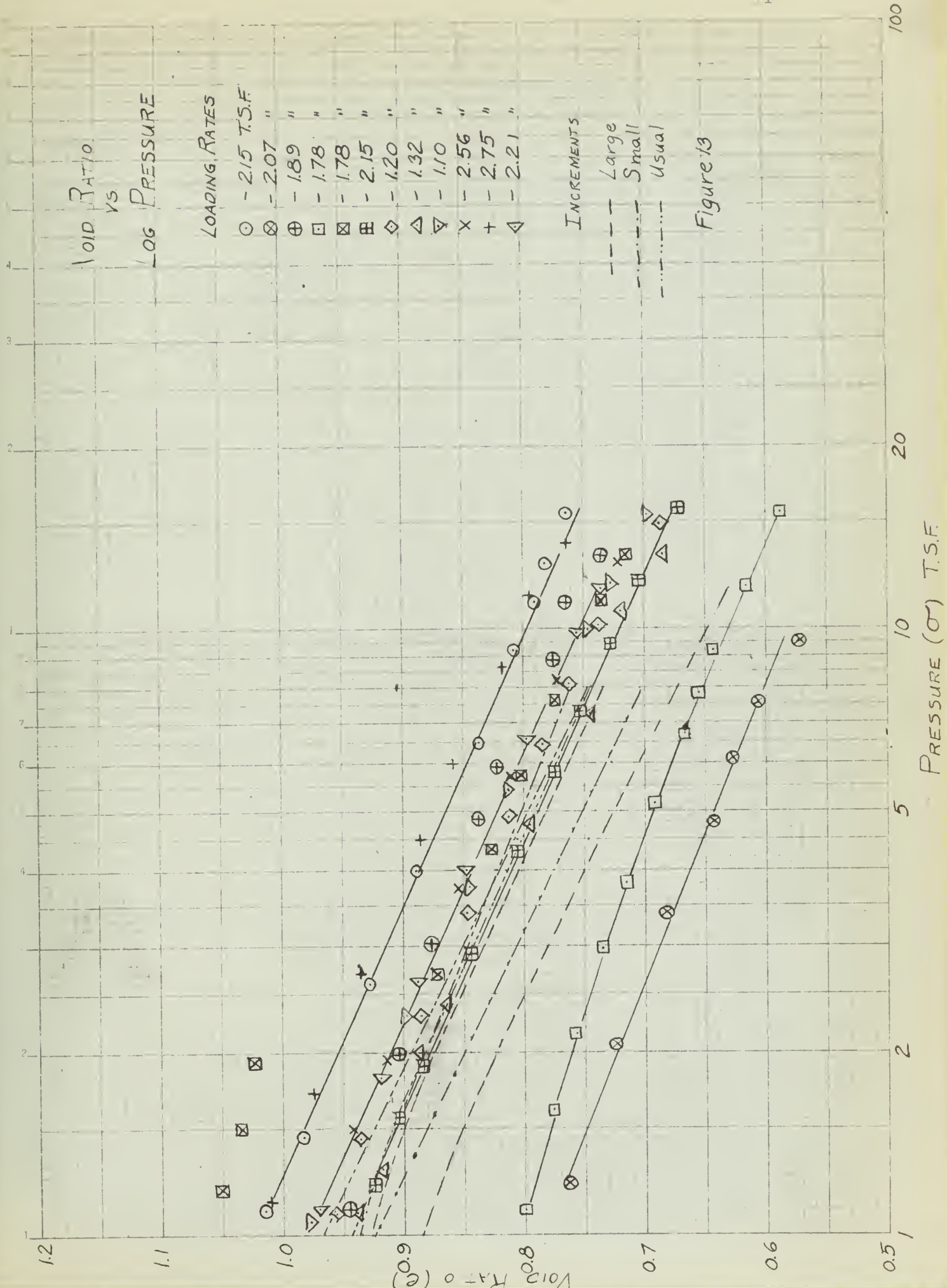
Consolidation readings were made directly, void ratio and porosity being computed from them. Permeability measurements were taken with the aid of a constant head manometer.

Figure 13 represents the standard "void ratio vs. logarithm of pressure" relationship. It can be seen that, with slight exception, the slopes of all the relatively straight lines are equal. In fact, for the fifteen test runs represented on this plot, the only factor that seems to govern the position of one curve relative to another is the initial void ratio. The values for void ratio at the commencement of these tests varied from approximately 1.000 to 1.400 and the values at the beginning of the plot varied from approximately 0.775 to 1.02. At the end of the plot the void ratio values varied from approximately .525 to .750, which fact indicates that little, if any, convergence or divergence of the curves occurs regardless of the rate of loading.

Figures 14 and 15 show the relationship of void ratio to time for the different loading rates. For static

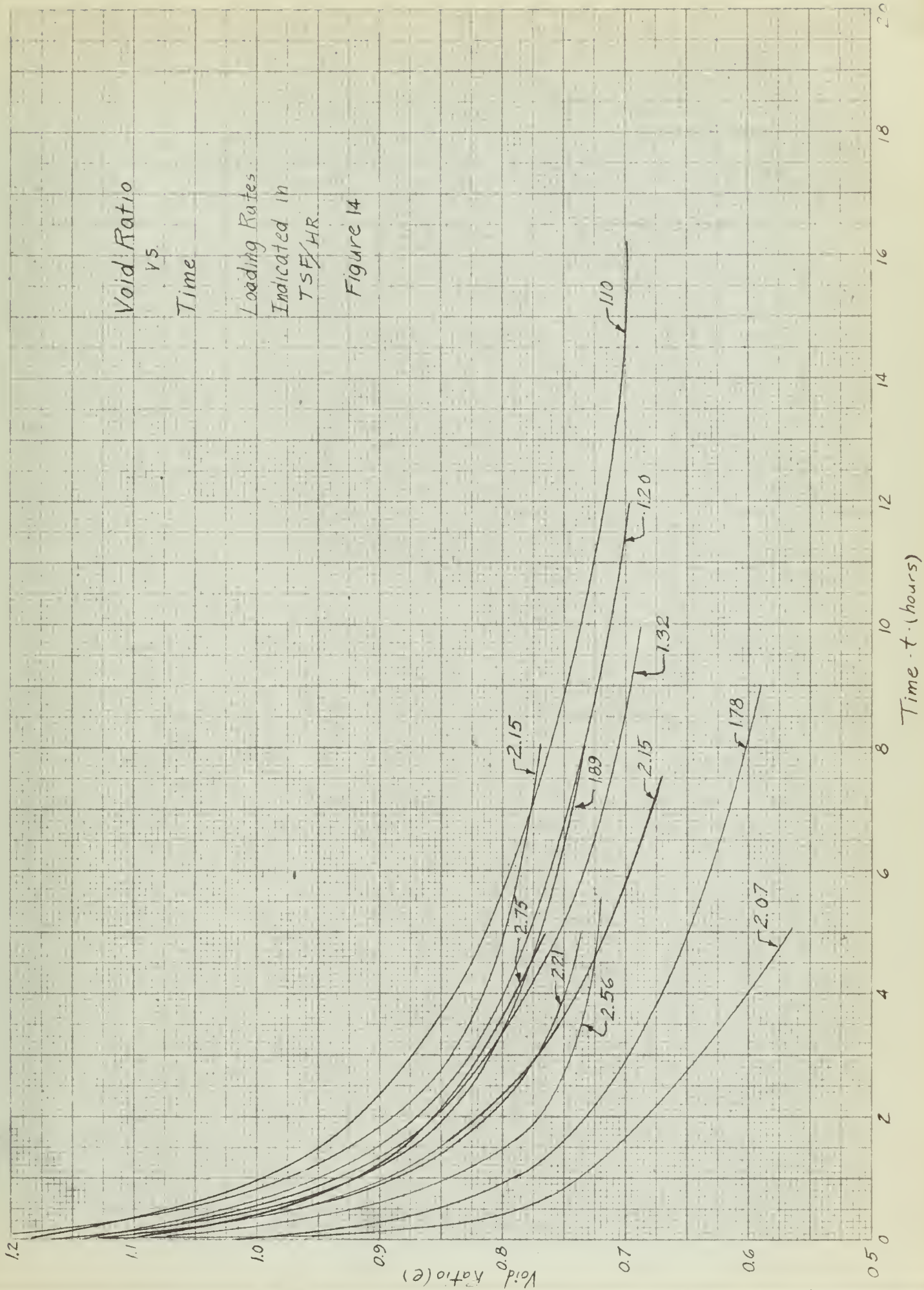


CP-1015-A 7-10-1958



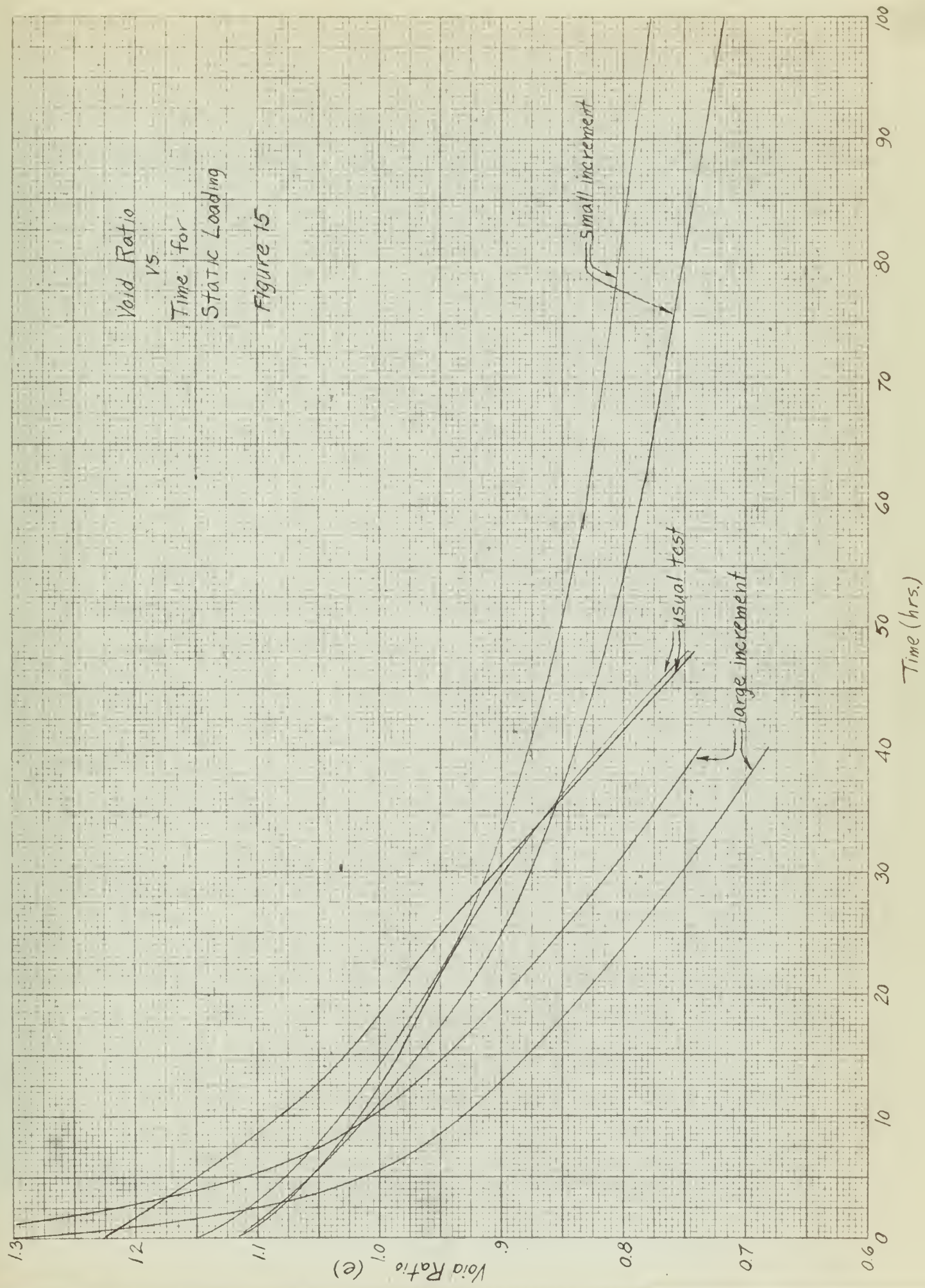
















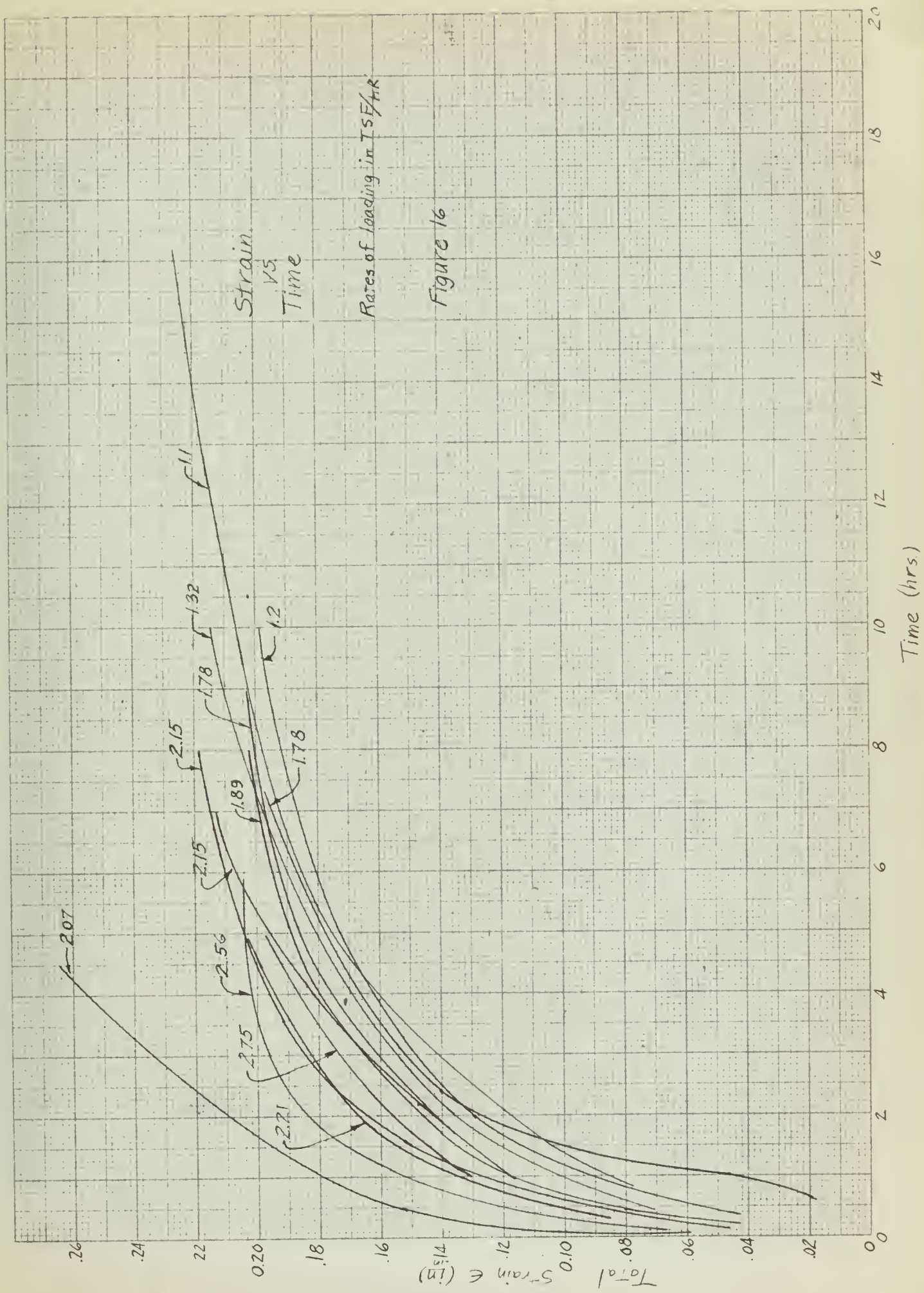
loadings it is seen that there is a definite trend toward smaller void ratio decrease with increase in load increment, although in each test the ultimate load was eight tons per square foot.

For the time-dependent (continuous-loading) tests, however, the results are not as conclusive. It is seen, though, that the more rapid loading rates are tending to approach an asymptote more rapidly and at a smaller void ratio change than the less rapid loading rates.

Figures 16 and 18 depict the relationship of total strain with time for different loading conditions. As can be gathered from the void ratio plot (Figures 14 and 15), the total deformation is shown to be greater for more rapid rates of loading. This is again illustrated on the plot for the static test where considerably greater total strains were experienced for large incremental test runs than for small incremental tests. The so-called usual test, which was used as a pilot study, has increments of loading between those of the other two series; however, in spite of the fact that these usual tests were subject to more error since technique was not fully developed at that early stage of testing, the plot of total strain falls between the two extremes of small increment and large increment.

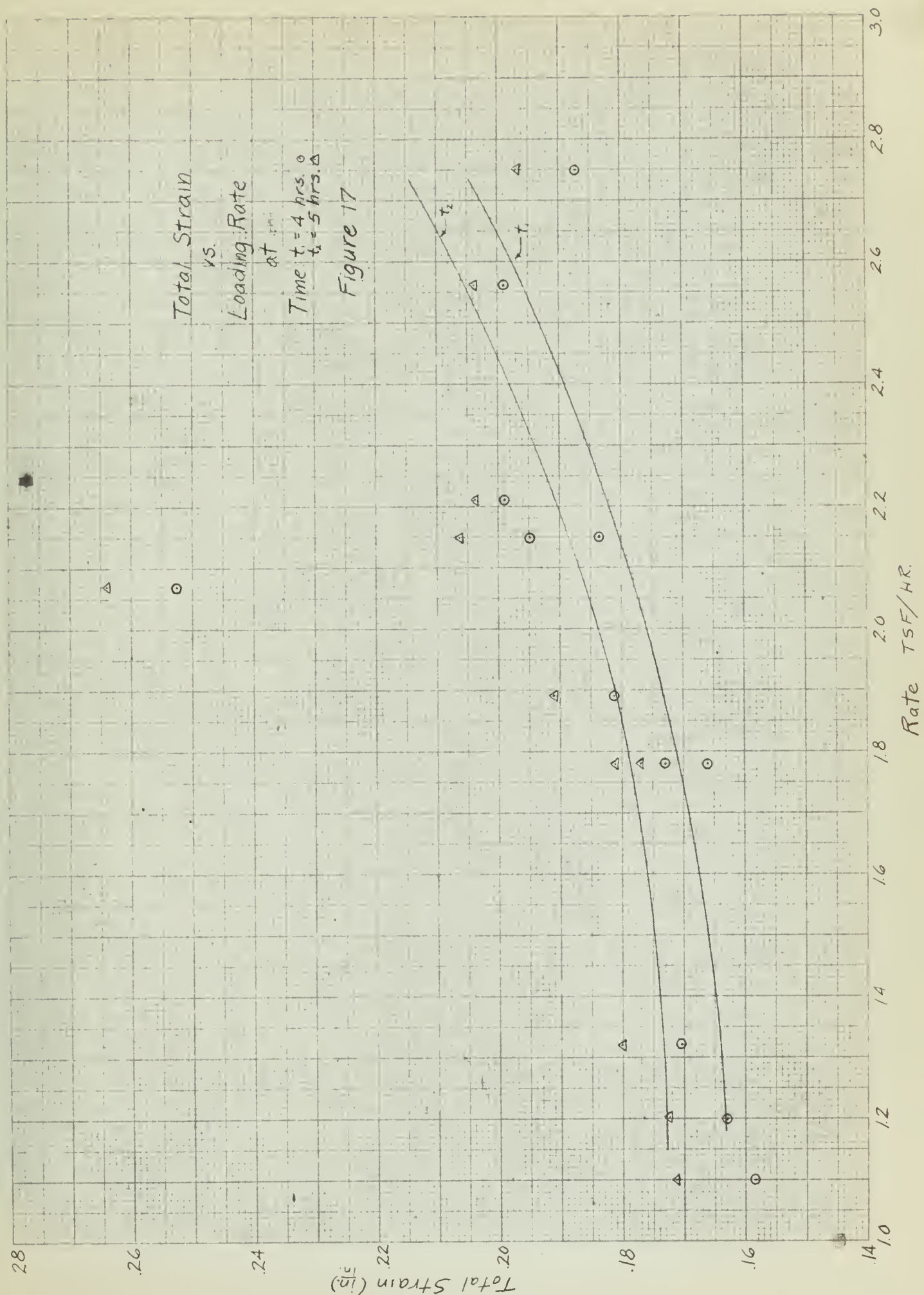
This effect is further illustrated by Figure 17 which is a plot of total strain versus rate-of-loading at a particular time during testing, in this case 4 hours.







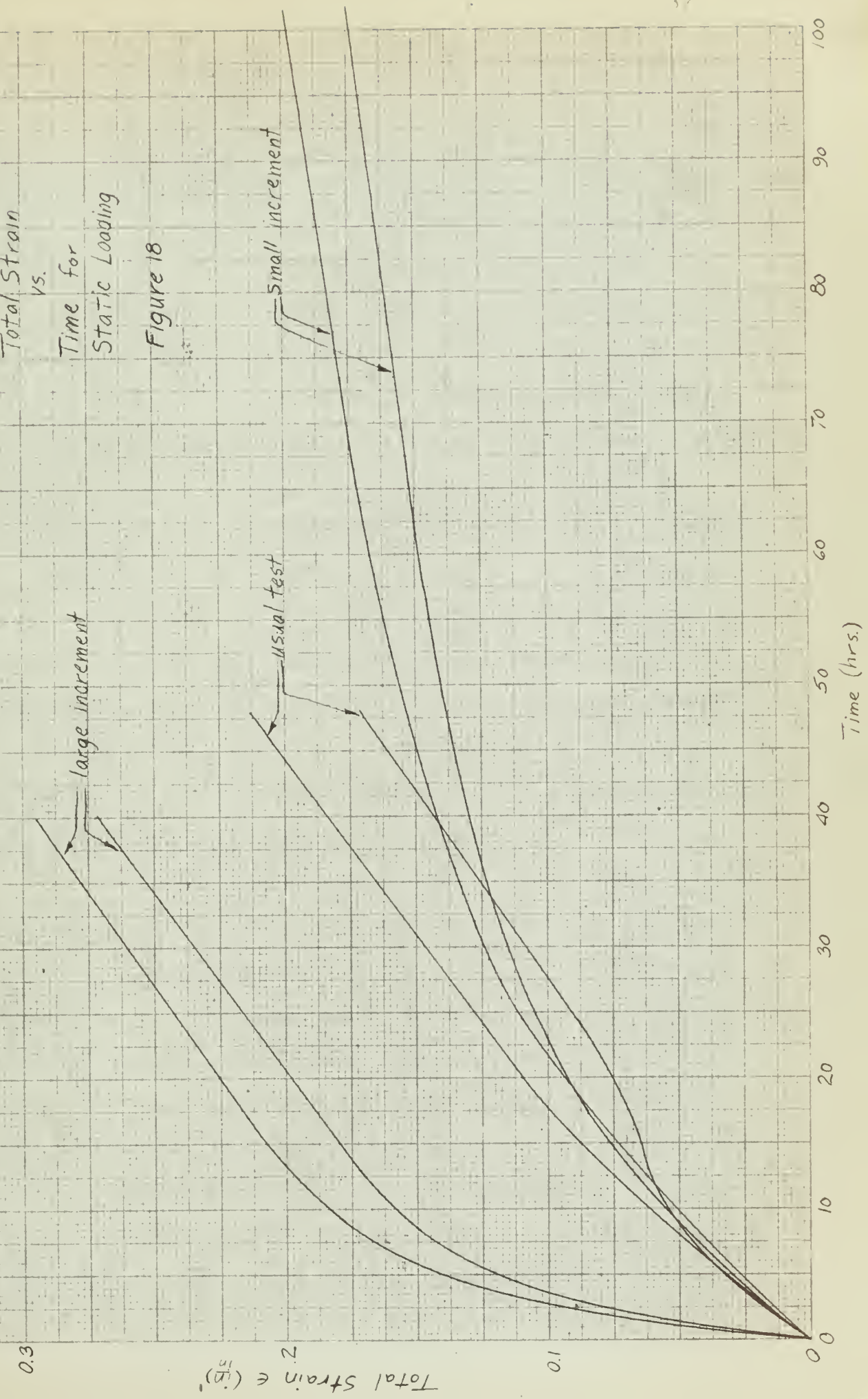






Total Strain  
vs.  
Time for  
Static Loading

Figure 18







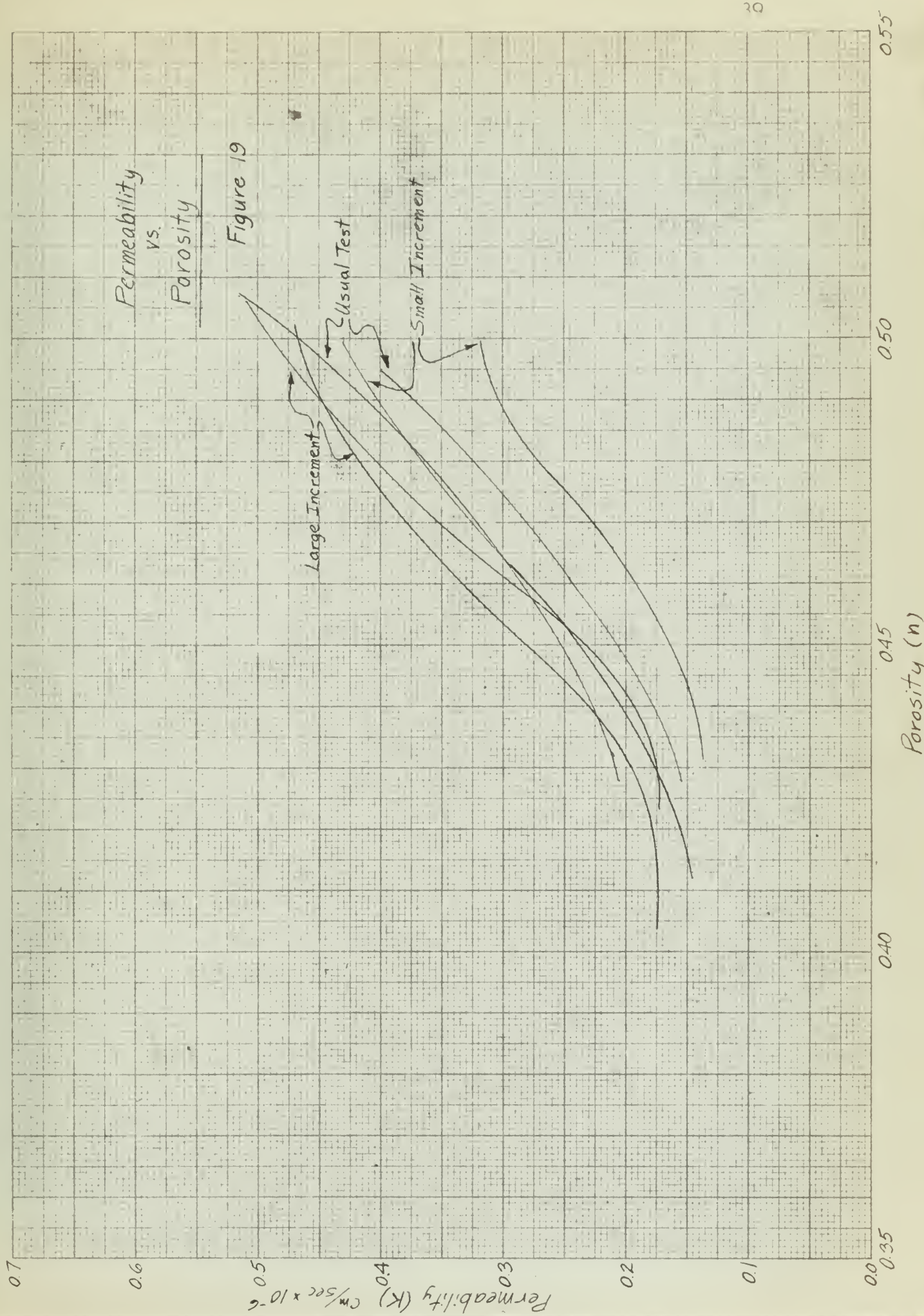
Although there is some scattering of points, the plotted curve seems to indicate that total strain increases at an ever-increasing amount as rate of loading increases.

Figures 19 and 20 are graphical representations of permeability versus porosity for various loading conditions. Although a total of thirteen test runs were accomplished with the continuous loading device, no definite relationship between permeability and porosity could be discovered. Since the only true permeability value was the one measured at the conclusion of loading, only one value could be plotted for each run. No two values were the same, even when the same rate of loading was applied. It must be noted, however, that the total spread between permeability values was from  $.083 \text{ cm/sec} \times 10^{-6}$  to  $0.12 \text{ cm/sec} \times 10^{-6}$  while the loading rates varied from 1.1 TSF/HR to 2.75 TSF/HR and the final load values varied from 11.60 TSF to 15.80 TSF.

For the static tests, however, a continuous curve could be plotted, since values for permeability were measured at the equilibrium point after every load increment. The curves plotted essentially parallel, and the permeability values for the large increment test runs were consistently larger than the values for the small increment test runs. Again, the usual test values lay between these two extremes.

A plot of permeability-versus-time for these same static tests (Figure 21) seems to substantiate the above results since there is a tendency for permeability to be









# PERMEABILITY VS. POROSITY

## LOADING RATES

|   |             |
|---|-------------|
| □ | 2.15 TSE/HR |
| ○ | 1.89 "      |
| ◇ | 1.78 "      |
| △ | 1.78 "      |
| ▽ | 2.15 "      |
| ◁ | 1.20 "      |
| ▷ | 1.32 "      |
| ⊗ | 1.70 "      |
| ⊕ | 2.50 "      |
| ⊞ | 2.75 "      |
| ⊠ | 2.21 "      |

FINAL LOADS INDICATED  
IN TONS PER SQ. FOOT

Figure 20

0.11

0.10

0.09

0.08

0.35

0.40

0.45

POROSITY (n)

11.60

15.80

13.20

13.28

14.80

15.15

13.80

13.25

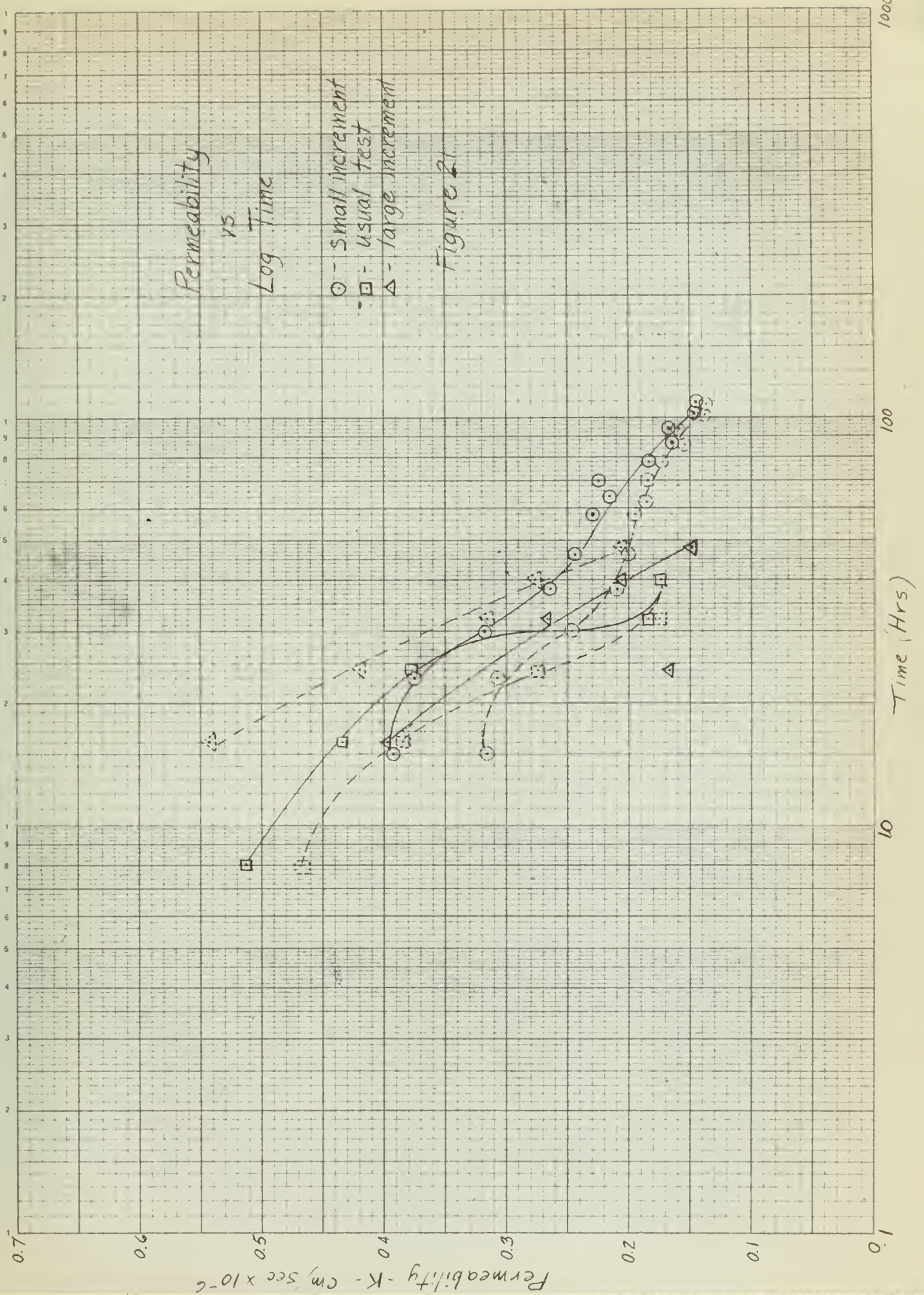
15.45

15.48

12.81











greater for the large incremental test than for the small incremental test with values for the usual test falling between these two extremes.



## PART VI.

## DISCUSSION

A. Static Tests

Six runs, two each of large increment, small increment and usual increment, were conducted in the series of static tests. Although these tests constituted a slight change from the standard consolidation tests, the course of testing was nonetheless followed at the suggestion of Mar-ron (4).

The results of the tests are both interesting and applicable. The fact that total strain and resultant void ratio decrease is larger for a large incremental load application could have far-reaching effects in construction. Most foundation designs are based on an allowable differential settlement. The fact that large increments of loading cause greater total consolidation than small increments of loading, even though the final total loads are equal, leads to the possibility of greater differential settlement under these large incremental conditions.

This phenomenon can probably be explained by hypothesizing that the smaller load increments cause less disturbance to the structure of the clay and concurrently allow more opportunity for the natural structure to develop than do the large increments. Therefore, it is conceivable that less total strain would take place if the structural



strength had built up to a greater extend under the smaller increments.

There are limitations to this concept, however, and far from the least of these is the fact that the study dealt with an ideal material, pure kaolinite. Of course, for the sake of study homogeneity simplifies the interpretation of results, but whether any field conditions approach this is another question entirely.

Figure 19 illustrates that the permeability is greater at time  $t$  and at porosity  $n$  for large increment than for small increment tests. It would seem, from the foregoing discussion, that the smaller increments would produce the large permeabilities since the total strain and void ratio change is less. Thus a question and a conflict arise.

It is readily seen that this line of testing presents interesting possibilities and certainly merits further research.



### B. Time-Dependent Loading Tests

Thirteen so-called continuous loading tests were conducted as a refinement of the standard static testing. Previous work by Marron (4) had been hampered by the lack of a dependent variable loading device. The electric motor--gear train--belt and pulley arrangement was a great improvement over his bubbler but is not the final answer. The valve stem of the air pressure regulator valve became extremely difficult to turn as the pressure was increased. Therefore, at relatively high pressures (40 psi) slippage of the belt on the pulleys occurred. As a result, pure time-dependent loading was not always obtained and the final pressures were not always as large as desired. A gear drive instead of the belt and pulley drive would solve this problem. Nevertheless, the tests as a whole proved quite satisfactory.

These tests seem to verify the results of the static tests in that the more rapid loading rates produced the greatest total strains and void ratio changes.

No such verification can be gathered from the plot of permeability versus porosity (Figure 19). The scattering of values is too random to permit the formulation of a general relationship. Perhaps if more time had been allowed to elapse after the discontinuation of additional loading before the reading of permeabilities, a relationship could be developed. Since there is such a small spread relatively, however, (from .083 to .12 cm/sec x  $10^{-6}$ ) a general





statement can be made. From the results of this series of tests there is relatively little effect upon permeability of rate of time-dependent loading.



### C. General

The results of these tests, although to some extent conclusive, bring to the author's mind many ideas for furthering the study.

A direct result of the time limitation is the factor of human error. In a research problem such as this the innumerable variables present in the raw material, in this case soil, are further compounded by the variation in technique of testing. Even though the soil samples are prepared with great diligence, no two samples are exactly alike. This alone accounts, more than likely, for most of the error in the test results. The plot of void ratio versus log of pressure (Figure 13) is a prime example. If the samples had all been prepared equally, the plot would have been one line.

Of course, the human error decreases as technique is improved and experience is gained.

If any further testing is contemplated, the following suggestions are offered:

- (1) The loading block of the consolidometer should be attached to the loading beam of the loading apparatus. This will eliminate much of the initial disturbance and early false readings caused by the relatively heavy weight of the block resting on the sample and yet not being included in the measured applied pressure.



- (2) A gear train should be fabricated to replace the belt and pulley drive. This will insure constant time-dependent loading.
- (3) The testing program should include series of tests at various rates of loading. At each rate of loading tests should be run from 0-1 TSF, 0-2 TSF, 0-3 TSF, up to 0-16 TSF. When each of these predetermined loads are reached, permeability readings should be taken after a predetermined waiting period to allow equilibrium to take place.
- (4) An automatic recording device (i.e., photographic) should be utilized especially during the initial half hour of testing. The process takes place too rapidly to permit accurate readings by eye. This record should include the manometer readings during the initial stages when water is forced back into the tube.



## PART VII.

## CONCLUSIONS

1. The utilization of an electric motor--gear train--belt and pulley device in conjunction with a Conbel loading apparatus is feasible and provides very good control in consolidation experiments.
2. There is a relationship between rate of loading and total consolidation. The larger the increment or the more rapid the rate of loading, the greater the total consolidation and the greater the resultant decrease in void ratio.
3. The fact that increment of loading does affect the permeability--porosity relationship is an indication that rate of loading does play a part. Although this same plot for the various rates of continuous loadings was inconclusive, certainly further study along this line is warranted.
4. The assumptions by Schiffman (5) that permeability is not constant under varying loading conditions during the consolidation process are valid.





## PART VIII.

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APPENDIX A

Sample Raw Data

Static Loading Tests



| Large Increment Static Loading |            |              |             |            |                         |       |                         |                     |              |                  |                                      | 23 Mar 59 |  |
|--------------------------------|------------|--------------|-------------|------------|-------------------------|-------|-------------------------|---------------------|--------------|------------------|--------------------------------------|-----------|--|
| Time                           | $\Delta T$ | Press<br>TST | Dial<br>in. | Ht.<br>in. | Vol.<br>in <sup>3</sup> | $V_s$ | $e = \frac{V}{V_s} - 1$ | $n = \frac{e}{1+e}$ | Perm<br>Gage | $\Delta Q$<br>cc | K<br>$\frac{cm}{sec} \times 10^{-6}$ |           |  |
| W = 43%                        | 0906       | 0.5          | 1150        | 1.0038     | 4.925                   | 2.137 | 1.305                   | .566                |              |                  |                                      |           |  |
|                                |            | 10           | 5130        | .9258      | 4.542                   |       | 1.125                   | .529                |              |                  |                                      |           |  |
|                                |            | 20           | 5180        | .9208      | 4.517                   |       | 1.114                   | .527                |              |                  |                                      |           |  |
|                                |            | 30           | 6020        | .9168      | 4.498                   |       | 1.105                   | .525                |              |                  |                                      |           |  |
|                                |            | 40           | 6050        | .9138      | 4.484                   |       | 1.098                   | .523                |              |                  |                                      |           |  |
|                                |            | 50           | 6070        | .9118      | 4.473                   |       | 1.093                   | .522                |              |                  |                                      |           |  |
|                                | 0907       | 1 m          | 6090        | .9098      | 4.463                   |       | 1.088                   | .521                |              |                  |                                      |           |  |
|                                |            | 1 1/2        | 6145        | .9043      | 4.436                   |       | 1.076                   | .518                |              |                  |                                      |           |  |
|                                | 0908       | 2            | 6185        | .9003      | 4.417                   |       | 1.067                   | .516                |              |                  |                                      |           |  |
|                                | 0909       | 3            | 7050        | .8938      | 4.385                   |       | 1.052                   | .513                |              |                  |                                      |           |  |
| 0910                           | 4          | 7100         | .8888       | 4.360      |                         | 1.045 | .510                    |                     |              |                  |                                      |           |  |
| 0911                           | 5          | 7130         | .8858       | 4.346      |                         | 1.034 | .508                    |                     |              |                  |                                      |           |  |
| 0916                           | 10         | 8048         | .8840       | 4.337      |                         | 1.029 | .507                    |                     |              |                  |                                      |           |  |
| 0926                           | 20         | 8137         | .8829       | 4.332      |                         | 1.027 | .506                    |                     |              |                  |                                      |           |  |
| 0936                           | 30         | 8190         | .8776       | 4.306      |                         | 1.015 | .504                    |                     |              |                  |                                      |           |  |
| 1006                           | 60         | 9033         | .8733       | 4.284      |                         | 1.005 | .501                    |                     |              |                  |                                      |           |  |
| 1106                           | 120        | 9053         | .8713       | 4.275      |                         | 1.000 | .500                    |                     |              |                  |                                      |           |  |
| 1306                           | 240        | 9069         | .8697       | 4.267      |                         | .997  | .499                    |                     |              |                  |                                      |           |  |
| 1645                           | 480        | 9077         | .8689       | 4.263      |                         | .995  | .498                    |                     |              |                  |                                      |           |  |
|                                |            |              |             |            |                         |       |                         |                     | 0.00         |                  |                                      |           |  |
|                                |            |              |             |            |                         |       |                         |                     | 0.40         | 0.40             | .416                                 |           |  |
|                                |            |              |             |            |                         |       |                         |                     | 0.90         | 0.50             | .520                                 |           |  |
|                                |            |              |             |            |                         |       |                         |                     | 1.35         | 0.45             | .468                                 |           |  |



| Large Increment Static Test |            |              |             |             |                 |                          |       |                         |                        |              |                  |  |
|-----------------------------|------------|--------------|-------------|-------------|-----------------|--------------------------|-------|-------------------------|------------------------|--------------|------------------|--|
| 24 Mar. '59                 |            |              |             |             |                 |                          |       |                         |                        |              |                  |  |
| Time                        | $\Delta T$ | Press<br>TSE | Dial<br>in. | Dial<br>in. | $\pi\pi$<br>in. | Vol.<br>in. <sup>3</sup> | $V_s$ | $e = \frac{V}{V_s} - 1$ | $\eta = \frac{e}{1+e}$ | Perm<br>Gage | $\Delta Q$<br>cc | $K$<br>$\frac{cm}{sec} \times 10^{-6}$ |
| 0859                        | 0 sec      | 1/2          | 9099        | 1893        | 8495            | 4.168                    | 2.137 | .950                    | .487                   | .42          |                  |  |
|                             | 10         |              | 9172        | 1972        | 8416            | 4.129                    |       | .932                    | .482                   |              |                  |  |
|                             | 20         |              | 9195        | 1995        | 8393            | 4.118                    |       | .927                    | .481                   | .10          |                  |  |
|                             | 30         |              | 10020       | 2020        | 8368            | 4.105                    |       | .921                    | .479                   |              |                  |  |
|                             | 40         |              | 10030       | 2030        | 8358            | 4.100                    |       | .919                    | .478                   |              |                  |  |
|                             | 50         |              | 10039       | 2039        | 8349            | 4.096                    |       | .917                    | .477                   |              |                  |  |
| 0900                        | 1 min.     |              | 10048       | 2048        | 8340            | 4.092                    |       | .914                    | .476                   | 0.0          |                  |  |
|                             | 1 1/2      |              | 10070       | 2070        | 8318            | 4.081                    |       | .910                    | .476                   | 0.0          |                  |  |
| 0901                        | 2          |              | 10082       | 2082        | 8306            | 4.075                    |       | .907                    | .475                   |              |                  |  |
| 0902                        | 3          |              | 10095       | 2095        | 8299            | 4.071                    |       | .905                    | .474                   |              |                  |  |
| 0903                        | 4          |              | 10102       | 2102        | 8292            | 4.068                    |       | .904                    | .474                   |              |                  |  |
| 0904                        | 5          |              | 10106       | 2106        | 8288            | 4.066                    |       | .903                    | .474                   |              |                  |  |
| 0909                        | 10         |              | 10115       | 2115        | 8279            | 4.062                    |       | .901                    | .474                   | .17          | .37              | 368                                    |
| 0919                        | 20         |              | 10122       | 2122        | 8272            | 4.058                    |       | .899                    | .473                   | .54          | .41              | 366                                    |
| 0929                        | 30         |              | 10126       | 2126        | 8268            | 4.056                    |       | .898                    | .473                   | .95          | .11              | 368                                    |
| 0959                        | 60         |              | 10132       | 2132        | 8262            | 4.055                    |       | .898                    | .473                   | 2.06         | 2.22             | 350                                    |
| 1059                        | 120        |              | 10138       | 2138        | 8256            | 4.050                    |       | .895                    | .472                   | 4.28         | 4.54             | 370                                    |
| 1259                        | 240        |              | 10145       | 2145        | 8248            | 4.046                    |       | .893                    | .472                   | 8.82         | 7.43             | 202                                    |
| 1622                        |            | 1            | 10150       | 2150        | 8243            | 4.044                    |       | .892                    | .471                   | 7.53         | .39              | 385                                    |
| 1632                        |            |              |             |             |                 |                          |       |                         |                        | 7.92         | .38              | 385                                    |
| 1642                        |            |              |             |             |                 |                          |       |                         |                        | 8.30         | .39              | 385                                    |
| 1652                        |            |              |             |             |                 |                          |       |                         |                        | 8.69         |                  | 385                                    |

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| Large Increment Static Test |            |              |            |            |            |                          |       |                       |                     |              |                  |  |
|-----------------------------|------------|--------------|------------|------------|------------|--------------------------|-------|-----------------------|---------------------|--------------|------------------|--|
| 25 Mar. '59                 |            |              |            |            |            |                          |       |                       |                     |              |                  |  |
| Time                        | $\Delta T$ | Press<br>TSF | Dial<br>in | Dial<br>in | Ht.<br>in. | Vol.<br>in. <sup>3</sup> | $V_s$ | $e = \frac{V-1}{V_s}$ | $n = \frac{e}{1+e}$ | Perm<br>Gage | $\Delta Q$<br>cc | $K$<br>$\frac{cm}{sec} \times 10^{-6}$ |
| 0836                        | 0 s        | 1            | 10181      | 2181       | 8207       | 4.026                    | 2.137 | .884                  | .469                | 2.38         |                  |  |
|                             | 10         |              | 11070      | 2270       | 8118       | 3.983                    |       | .864                  | .464                |              |                  |  |
|                             | 20         |              | 11109      | 2309       | 8079       | 3.963                    |       | .854                  | .461                |              |                  |  |
|                             | 30         |              | 11134      | 2334       | 8054       | 3.951                    |       | .849                  | .459                |              |                  |  |
|                             | 40         |              | 11153      | 2353       | 8035       | 3.942                    |       | .845                  | .458                |              |                  |  |
|                             | 50         |              | 11166      | 2366       | 8022       | 3.936                    |       | .842                  | .457                |              |                  |  |
| 0837                        | 1 m.       |              | 11176      | 2376       | 8012       | 3.931                    |       | .839                  | .456                | 1.72         |                  |  |
|                             | 1 1/2      |              | 11196      | 2396       | 7992       | 3.921                    |       | .835                  | .455                | 1.69         |                  |  |
| 0838                        | 2          |              | 12005      | 2405       | 7983       | 3.916                    |       | .832                  | .454                | 1.68         |                  |  |
| 0839                        | 3          |              | 12014      | 2414       | 7974       | 3.912                    |       | .831                  | .454                |              |                  |  |
| 0840                        | 4          |              | 12018      | 2418       | 7972       | 3.911                    |       | .830                  | .453                | 1.70         | .02              | .191                                   |
| 0841                        | 5          |              | 12022      | 2422       | 7968       | 3.909                    |       | .829                  | .452                | 1.72         | .02              | .191                                   |
| 0846                        | 10         |              | 12028      | 2428       | 7962       | 3.906                    |       | .828                  | .452                | 1.83         | .02              | .210                                   |
| 0856                        | 20         |              | 12034      | 2434       | 7956       | 3.903                    |       | .826                  | .452                | 2.10         | .11              | .258                                   |
| 0906                        | 30         |              | 12038      | 2438       | 7952       | 3.901                    |       | .825                  | .452                | 2.36         | .26              | .257                                   |
| 0936                        | 60         |              | 12045      | 2445       | 7949       | 3.900                    |       | .825                  | .452                | 3.19         | .83              | .264                                   |
| 1036                        | 120        |              | 12050      | 2450       | 7944       | 3.897                    |       | .824                  | .452                | 4.75         | 1.56             | .247                                   |
| 1236                        | 240        |              | 12055      | 2455       | 7939       | 3.895                    |       | .824                  | .452                | 8.25         | 3.50             | .277                                   |
| 1545                        |            | 2            | 12063      | 2463       | 7931       | 3.891                    |       | .821                  | .451                | 5.35         | 5.15             | .159                                   |
| 1555                        |            |              |            |            |            |                          |       |                       |                     | 5.75         | .40              | .274                                   |
| 1605                        |            |              |            |            |            |                          |       |                       |                     | 6.15         | .40              | .274                                   |

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Refilled to 0.2 cc.



| Large Increment Static Test |        |              |            |            |           |                          |       |                       |                     | 26 Mar '59    |          |                                     |
|-----------------------------|--------|--------------|------------|------------|-----------|--------------------------|-------|-----------------------|---------------------|---------------|----------|-------------------------------------|
| Time                        | ΔT     | Press<br>TSF | Dial<br>in | Dial<br>in | Ht<br>in. | Vol.<br>in. <sup>3</sup> | Vs    | $C = \frac{V}{B} - 1$ | $n = \frac{Q}{H+E}$ | Perm.<br>Gage | ΔQ<br>cc | $k = \frac{cm}{sec} \times 10^{-6}$ |
| 0808                        | 0 sec  | 2            | 12087      | 2487       | 7901      | 3.876                    | 2.137 | .814                  | .449                | 1.31          |          |                                     |
|                             | 10     |              | 13000      | 2600       | 7788      | 3.821                    |       | .788                  | .441                | 95            |          |                                     |
|                             | 20     |              | 13041      | 2641       | 7747      | 3.807                    |       | .781                  | .439                | 86            |          |                                     |
|                             | 30     |              | 13067      | 2667       | 7721      | 3.788                    |       | .773                  | .436                | 78            |          |                                     |
|                             | 40     |              | 13083      | 2683       | 7705      | 3.780                    |       | .769                  | .435                | 73            |          |                                     |
|                             | 50     |              | 13094      | 2694       | 7694      | 3.775                    |       | .766                  | .434                | 71            |          |                                     |
| 0809                        | 1 min. |              | 13101      | 2701       | 7687      | 3.771                    |       | .765                  | .433                | 69            |          |                                     |
|                             | 1 1/2  |              | 13113      | 2713       | 7675      | 3.765                    |       | .762                  | .432                | 67            |          |                                     |
| 0810                        | 2      |              | 13117      | 2717       | 7671      | 3.763                    |       | .761                  | .432                | 65            |          | .184                                |
| 0811                        | 3      |              | 13123      | 2723       | 7666      | 3.761                    |       | .760                  | .432                | 69            | .02      | .184                                |
| 0812                        | 4      |              | 13126      | 2726       | 7663      | 3.759                    |       | .759                  | .432                | 70            | .01      | .092                                |
| 0813                        | 5      |              | 13128      | 2728       | 7661      | 3.758                    |       | .758                  | .432                | 80            | .10      | .184                                |
| 0818                        | 10     |              | 13135      | 2735       | 7654      | 3.755                    |       | .756                  | .431                | 1.00          | .20      | .183                                |
| 0828                        | 20     |              | 13140      | 2740       | 7649      | 3.753                    |       | .754                  | .431                | 1.25          | .25      | .229                                |
| 0838                        | 30     |              | 13144      | 2744       | 7645      | 3.751                    |       | .754                  | .431                | 1.90          | .65      | .198                                |
| 0908                        | 60     |              | 13149      | 2749       | 7640      | 3.748                    |       | .754                  | .430                | 3.20          | 1.30     | .198                                |
| 1008                        | 120    |              | 13154      | 2754       | 7635      | 3.746                    |       | .752                  | .430                | 5.90          | 2.70     | .206                                |
| 1208                        | 240    |              | 13160      | 2760       | 7629      | 3.743                    |       |                       | .430                | 7.60          | 1.70     | .216                                |
| 1320                        |        | 4            | 13166      | 2766       | 7623      | 3.740                    |       | .750                  | .429                | 2.55          | 2.15     | .123                                |
| 1500                        |        |              |            |            |           |                          |       |                       |                     | 2.74          | .19      | .174                                |
| 1510                        |        |              |            |            |           |                          |       |                       | .429                | 2.94          | .20      | .175                                |
| 1520                        |        |              |            |            |           |                          |       |                       |                     |               |          |                                     |

Refilled to 0.4 cc.



| Large Increment Static Test |            |              |             |           |                         |               |                     |                     |              |                  | 27 Mar. '59                         |
|-----------------------------|------------|--------------|-------------|-----------|-------------------------|---------------|---------------------|---------------------|--------------|------------------|-------------------------------------|
| Time                        | $\Delta T$ | Press<br>TSF | Dial<br>in. | HT<br>in. | Vol.<br>in <sup>3</sup> | $\frac{1}{s}$ | $e = \frac{L-1}{L}$ | $n = \frac{e}{1+e}$ | Perm<br>Gage | $\Delta Q$<br>cc | K<br>$\frac{cm}{sec} \cdot 10^{-6}$ |
| 1010                        | 0 sec      | 4            | 13187       | 2787      | 7601                    | 3.729         | 2.137               | .745                | 3.95         |                  |                                     |
|                             | 10         |              | 14125       | 2925      | 7463                    | 3.661         |                     | .713                |              |                  |                                     |
|                             | 20         |              | 14165       | 2965      | 7423                    | 3.642         |                     | .704                |              |                  |                                     |
|                             | 30         |              | 14190       | 2990      | 7398                    | 3.629         |                     | .698                | 3.30         |                  |                                     |
|                             | 40         |              | 15000       | 3000      | 7388                    | 3.625         |                     | .696                |              |                  |                                     |
|                             | 50         |              | 15009       | 3009      | 7379                    | 3.620         |                     | .694                |              |                  |                                     |
| 1011                        | 1 min.     |              | 15013       | 3013      | 7375                    | 3.618         |                     | .693                | 3.23         |                  |                                     |
| 1012                        | 1 1/2      |              | 15020       | 3020      | 7368                    | 3.615         |                     | .692                | 3.22         |                  |                                     |
| 1013                        | 2          |              | 15025       | 3025      | 7363                    | 3.612         |                     | .691                | 3.22         |                  |                                     |
| 1014                        | 3          |              | 15029       | 3029      | 7359                    | 3.610         |                     | .689                | 3.23         | .01              | .880                                |
| 1015                        | 4          |              | 15032       | 3032      | 7355                    | 3.608         |                     | .688                | 3.24         | .01              | .880                                |
| 1015                        | 5          |              | 15034       | 3034      | 7353                    | 3.607         |                     | .688                | 3.25         | .01              | .880                                |
| 1020                        | 10         |              | 15040       | 3040      | 7347                    | 3.604         |                     | .686                | 3.32         | .07              | .123                                |
| 1030                        | 20         |              | 15045       | 3045      | 7342                    | 3.602         |                     | .685                | 3.48         | .16              | .141                                |
| 1040                        | 30         |              | 15049       | 3049      | 7338                    | 3.600         |                     | .685                | 3.64         | .16              | .141                                |
| 1110                        | 60         |              | 15054       | 3054      | 7333                    | 3.598         |                     | .684                | 4.17         | .53              | .155                                |
| 1210                        | 120        |              | 15060       | 3060      | 7327                    | 3.595         |                     | .683                | 5.25         | 1.08             | .158                                |
| 1410                        | 240        | 8            | 15065       | 3065      | 7322                    | 3.592         |                     | .681                | 7.30         | 2.05             | .151                                |
| 1645                        |            |              | 15070       | 3070      | 7317                    | 3.590         |                     | .680                | 2.50         | 2.50             | .142                                |
| 1655                        |            |              |             |           |                         |               |                     |                     | 2.70         | .20              | .175                                |
| 1705                        |            |              |             |           |                         |               |                     |                     | 2.90         | .20              | .175                                |

Refilled to 0.00

Final.

Can # 55 - 13.1532  
 + Net - 135.4617  
 - Dry - 105.2329  
 W = 32.8%  
 Vol. =



# SAMPLE CALCULATIONS

$$Q = KIA$$

$$K = \frac{Q}{IA} = \frac{\Delta Q}{(t \cdot \frac{L}{H} \cdot A)} = \frac{\Delta Q \cdot L}{t \cdot H \cdot A}$$

$\Delta Q$  = flow of water (c.c) during time  $t$

$t$  = time (seconds)

$L$  = average length of sample over time  $t$  (in.)

$H$  = head of permeameter (116.6 cm)

$A$  = area of sample (4.906 in<sup>2</sup>)

$K$  = coefficient of permeability (cm./sec.  $\times 10^{-6}$ )

$$K = \frac{\Delta Q}{t} \times \frac{L \cdot 2.54}{116.6 \cdot 4.906 \cdot (2.54)^2} = 0.00688 \times \frac{\Delta Q \cdot L}{t}$$

$$= .688 \times 10^{-3} \times \frac{\Delta Q \cdot L}{t} \text{ cm./sec.}$$





## APPENDIX B

Sample Raw DataTime-Dependent Loading Tests



| Continuous Loading Test #1   |      |            |           |            |          |          |         |          |                           |                 | 16 Feb. 59 |               |                        |
|--|------|------------|-----------|------------|----------|----------|---------|----------|---------------------------|-----------------|------------|---------------|------------------------|
| Rate: 2.15 TSF/HR  | Time | Press. PSI | (-) Corr. | Press. TSF | Dial in. | Dial in. | Hr. in. | Vol. in. | C = $\frac{V}{A \cdot L}$ | $\frac{e}{1+e}$ | Perm Gage  | $\Delta Q$ cc | $K_{comp} \times 10^3$ |
| Initial Meas.<br>Can #66<br>Tare: 13.0658<br>+ Wet: 23.9983<br>+ Dry: 24.2391<br>W = 42.7%                           | 0845 | 0.5        | 0         | 0          | 15.184   | 3184     | 0065    | 4.938    | 1.259                     | 557             | 0.5        |               |                        |
|  | 0854 | 0.7        | 0         | .10        | 15.00    | 3100     | 9981    | 4.897    | 1.270                     | 554             |            |               |                        |
|  | 0856 | 0.7        | .1        | .13        | 14.80    | 2985     | 9861    | 4.838    | 1.213                     | 548             |            |               |                        |
|  | 0900 | 1.0        | .2        | .15        | 13.86    | 2780     | 9661    | 4.743    | 1.168                     | 539             |            |               |                        |
|  | 0908 | 1.8        | .3        | .45        | 13.084   | 2684     | 9565    | 4.693    | 1.147                     | 534             |            |               |                        |
|  | 0918 | 3.0        | .5        | .80        | 11.050   | 2250     | 9131    | 4.480    | 1.049                     | 512             |            |               |                        |
|  | 0924 | 3.3        | .5        | .90        | 10.170   | 2170     | 9051    | 4.440    | 1.031                     | 508             |            |               |                        |
|  | 0930 | 4.0        | .5        | 1.10       | 10.100   | 2100     | 8981    | 4.406    | 1.016                     | 504             |            |               |                        |
|  | 0938 | 4.8        | .6        | 1.33       | 10.03    | 2003     | 8884    | 4.358    | .994                      | 498             |            |               |                        |
|  | 0942 | 5.2        | .5        | 1.45       | 9.153    | 1953     | 8834    | 4.334    | .983                      | 496             |            |               |                        |
| Final Meas<br>Can #44<br>Tare: 9.7275<br>+ Wet: 13.3710<br>+ Dry: 10.38942<br>W = 31.7%<br>Vol. 3.945 m <sup>3</sup> | 0948 | 5.8        | .7        | 1.62       | 9.115    | 1915     | 8796    | 4.315    | .974                      | 493             |            |               |                        |
|  | 1000 | 6.3        | .8        | 1.75       | 9.008    | 1808     | 8689    | 4.263    | .950                      | 491             |            |               |                        |
|  | 1015 | 9.0        | .8        | 2.63       | 8.110    | 1710     | 8591    | 4.215    | .928                      | 48              |            |               |                        |
|  | 1025 | 9.9        | .8        | 2.82       | 8.060    | 1660     | 8541    | 4.190    | .917                      | 478             |            |               |                        |
|  | 1030 | 10.5       | .9        | 3.00       | 8.033    | 1633     | 8514    | 4.177    | .911                      | 477             |            |               |                        |
|  | 1042 | 11.9       | .9        | 3.62       | 7.181    | 1581     | 8422    | 4.151    | .899                      | 473             |            |               |                        |
|  | 1052 | 13.1       | .9        | 4.00       | 7.10     | 1540     | 8421    | 4.130    | .889                      | 471             |            |               |                        |
|  | 1100 | 14.0       | 1.0       | 4.30       | 7.10     | 1514     | 8395    | 4.119    | .884                      | 460             |            |               | .035                   |
|  | 1122 | 16.6       | 1.0       | 5.12       | 7.031    | 1431     | 8312    | 4.078    | .866                      | 464             |            |               | .041                   |
|  | 1150 | 19.7       | 1.0       | 6.20       | 6.152    | 1352     | 8293    | 4.026    | .842                      | 457             |            |               | .066                   |
| Bellows Cont'd To One Dice   | 1200 | 20.6       | 1.0       | 6.50       | 6.130    | 1330     | 8211    | 4.015    | .837                      | 456             |            |               | .035                   |
|  | 1215 | 22.4       | 1.0       | 7.10       | 6.094    | 1294     | 8175    | 4.011    | .835                      | 455             |            |               | .041                   |
|  | 1234 | 24.4       | 1.1       | 7.70       | 6.053    | 1253     | 8134    | 3.991    | .826                      | 452             |            |               | .066                   |
|  | 1251 | 26.4       | 1.1       | 8.40       | 6.020    | 1220     | 8101    | 3.974    | .818                      | 450             |            |               | .070                   |
|  | 1310 | 29.0       | 1.1       | 9.25       | 5.170    | 1170     | 8051    | 3.950    | .807                      | 447             |            |               | .072                   |
|  | 1330 | 31.0       | 1.1       | 9.98       | 5.154    | 1154     | 8036    | 3.942    | .803                      | 440             |            |               |                        |
|  | 1345 | 32.6       | 1.2       | 10.40      | 5.122    | 1122     | 8023    | 3.926    | .796                      | 443             |            |               |                        |
|  | 1400 | 34.5       | 1.2       | 11.05      | 5.090    | 1096     | 7977    | 3.914    | .790                      | 441             |            |               |                        |
|  | 1505 | 35.4       | 1.2       | 11.33      | 5.060    | 1096     | 7977    | 3.914    | .790                      | 441             |            |               |                        |
|  | 1520 | 37.0       | 1.2       | 11.30      | 5.081    | 1081     | 7962    | 3.906    | .787                      | 440             |            |               |                        |



| Continuous Loading Test #9 |              |              |            |            |           |                         |                |                         |                     |              |                  |                      |
|----------------------------|--------------|--------------|------------|------------|-----------|-------------------------|----------------|-------------------------|---------------------|--------------|------------------|----------------------|
| Time                       | Press<br>PSI | (-)<br>Corr. | Dial<br>in | Dial<br>in | Ht<br>in. | Vol.<br>in <sup>3</sup> | V <sub>s</sub> | $e = \frac{V}{V_s} - 1$ | $n = \frac{e}{1+e}$ | Perm<br>Gage | $\Delta Q$<br>cc | $K = \frac{cm}{sec}$ |
| 0908                       | 3            | 0            | 1712       | 3520       | 1.065     | 4.938                   | 2.303          | 1.144                   | .533                |              |                  |                      |
| 0910                       | 5            | 0            | 17075      | 3475       | 1.0020    | 4.916                   |                | 1.135                   | .532                |              |                  |                      |
| 0912                       | 6            | 0.1          | 17010      | 3410       | .9955     | 4.884                   |                | 1.121                   | .529                |              |                  |                      |
| 0917                       | 9            | 0.1          | 16070      | 3270       | .9815     | 4.815                   |                | 1.091                   | .522                |              |                  |                      |
| 0920                       | 1.1          | 0.2          | 15181      | 3186       | .9725     | 4.771                   |                | 1.072                   | .517                |              |                  |                      |
| 0923                       | 1.3          | 0.2          | 15108      | 3108       | .9653     | 4.736                   |                | 1.056                   | .514                |              |                  |                      |
| 0931                       | 1.8          | 0.3          | 14133      | 2933       | .9478     | 4.650                   |                | 1.019                   | .505                |              |                  |                      |
| 0937                       | 2.1          | 0.4          | 14035      | 2835       | .9380     | 4.602                   |                | .998                    | .499                |              |                  |                      |
| 0941                       | 2.4          | 0.4          | 14003      | 2800       | .9345     | 4.585                   |                | .990                    | .497                |              |                  |                      |
| 0946                       | 2.7          | 0.4          | 13144      | 2744       | .9289     | 4.557                   |                | .979                    | .495                |              |                  |                      |
| 0952                       | 3.1          | 0.5          | 13074      | 2674       | .9219     | 4.523                   |                | .964                    | .491                |              |                  |                      |
| 1004                       | 3.9          | 0.5          | 12162      | 2562       | .9117     | 4.468                   |                | .940                    | .485                |              |                  |                      |
| 1010                       | 4.3          | 0.6          | 12109      | 2509       | .9054     | 4.442                   |                | .929                    | .482                |              |                  |                      |
| 1017                       | 4.7          | 0.6          | 12063      | 2460       | .9005     | 4.418                   |                | .918                    | .479                |              |                  |                      |
| 1030                       | 5.8          | 0.6          | 11112      | 2372       | .8917     | 4.375                   |                | .900                    | .474                |              |                  |                      |
| 1045                       | 6.9          | 0.7          | 11087      | 2287       | .8832     | 4.333                   |                | .881                    | .468                |              |                  |                      |
| 1100                       | 8.0          | 0.7          | 11011      | 2211       | .8756     | 4.296                   |                | .865                    | .464                |              |                  |                      |
| 1115                       | 9.2          | 0.8          | 10140      | 2140       | .8685     | 4.261                   |                | .850                    | .459                |              |                  |                      |
| 1236                       | 15.3         | 0.9          | 9386       | 1886       | .8431     | 4.136                   |                | .796                    | .443                |              |                  |                      |
| 1300                       | 17.3         | 0.9          | 9032       | 1832       | .8577     | 4.110                   |                | .785                    | .440                |              |                  |                      |
| 1430                       | 24.3         | 1.0          | 8060       | 1600       | .8205     | 4.025                   |                | .748                    | .428                |              |                  |                      |
| 1601                       | 31.3         | 1.0          | 7129       | 1529       | .8074     | 3.961                   |                | .720                    | .419                |              |                  |                      |
| 1630                       | 33.4         | 1.1          | 7094       | 1494       | .8039     | 3.944                   |                | .712                    | .416                |              |                  |                      |
| 1655                       | 35.1         | 1.1          | 7067       | 1467       | .8012     | 3.931                   |                | .707                    | .414                |              |                  |                      |
| 1819                       | 46.8         | 1.2          | 6184       | 1384       | .7929     | 3.890                   |                | .689                    | .408                |              |                  |                      |
| 1902                       | 41.0         | 1.2          | 6174       | 1374       | .7919     | 3.885                   |                | .687                    | .407                |              |                  |                      |
| 2030                       | 41.0         | 1.2          | 6165       | 1365       | .7910     | 3.881                   |                | .685                    | .407                |              |                  |                      |
| 2040                       | 41.0         | 1.2          | 6165       | 1365       | .7910     | 3.890                   |                | .685                    | .407                |              |                  |                      |
| 2050                       | 41.0         | 1.2          | 6165       | 1365       | .7910     | 3.885                   |                | .685                    | .407                |              |                  |                      |
| 2100                       | 41.0         | 1.2          | 6165       | 1365       | .7910     | 3.881                   |                | .685                    | .407                |              |                  |                      |

Rate = 1.32 TSP  
Hr.

Initial Meas.  
Can #66  
Tare: 13.0658  
+ Wet: 25.2785  
+ Dry: 21.5965  
W = 43.1%

Final Meas  
Can #41  
Tare: 9.7258  
+ Wet: 140.5720  
+ Dry: 108.9952  
W = 31.8%

Vol =











thesW5552

A study of the effects of varying rates



3 2768 001 95070 2

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